

Selective Adaptation in Networks of Heterogeneous Populations: Model, Simulation and Experiment

Avner Wallach¹, Danny Eytan¹, Shimon Marom², Ron Meir¹

Faculties of Electrical Engineering¹ and Medicine²,
Technion Israel Institute of Technology, Haifa, Israel.

Abstract

Biological systems often change their responsiveness when subject to persistent stimulation, a phenomenon termed adaptation. In neural systems this process is often selective, allowing the system to adapt to one stimulus while preserving its sensitivity to another. In some studies it has been shown that adaptation to a frequent stimulus increases the system's sensitivity to rare stimuli. These phenomena were explained in previous work as a result of complex interactions between the various sub-populations of the network. A formal description and analysis of neuronal systems, however, is hindered by the network's heterogeneity and by the multitude of processes taking place at different time-scales. Viewing neural networks as populations of interacting elements, we develop a framework that facilitates a formal analysis of complex, structured, heterogeneous networks. The formulation developed is based on an analysis of the availability of activity dependent resources, and their effects on network responsiveness. This approach offers a simple mechanistic explanation for selective adaptation, and leads to several predictions which were corroborated in both computer simulations and in cultures of cortical neurons developing *in-vitro*. The framework is sufficiently general to apply to different biological systems, and was demonstrated in two different cases.

Author Summary

Our mind continuously adapts to background sensory events while preserving and even enhancing its sensitivity to deviant objects. In the visual modality, for instance, a target violating a surrounding pattern is easily detected, a phenomenon termed 'pop-out'. Indeed, the automatic attention we pay to the irregular or the surprising, which developed as a valuable aid in our survival, is often used to advantage nowadays in popular culture and advertisement. Such phenomena have been investigated in many systems, from psychophysics in behaving animals to experiments in neural networks developing *in-vitro*. In this work we develop a mechanistic model which demonstrates how a relatively simple system may express such selective behavior. We apply our model first to the case of transiently responding networks, and compare the results with computer simulations and experimental data collected from neural networks developing *in-vitro*. We also demonstrate the application of the model to other systems. Our approach provides insight as to how complex, behavior-related phenomena may arise from simple dynamic interactions between the system's elementary components.

Introduction

Adaptation is a biologically ubiquitous process whereby features of a system's responsiveness change as a result of previous input. In neural systems, the kinetics of the change are most often monotonic and its direction (either increase or decrease) depends on the information conveyed and on the identity of the biological components observed (e.g. [1-3]). It has been shown that neural adaptation is inherently selective to the input characteristics; not only between sensory modalities, but even within a given modality, the system is capable of reducing its sensitivity to frequent input while preserving its sensitivity to the rare (e.g. [3-8]). In its most impressive form, the phenomenon of selective adaptation also contains an increased sensitivity to the rare on the background of frequent input. For instance, in the phenomenon of Mismatch Negativity (MMN), when a deviant sensory stimulus is applied on the background of a standard one, an evoked potential component which is absent in the presence of a single stimulus (e.g. [6,9,10]) is generated. This component's magnitude was shown to depend on the scarcity of the odd-ball stimulus and on the rate of stimulation.

To simplify matters, adaptation can be viewed as a result of a dynamic interaction between exciting and restoring forces: the monotonic nature of adaptation, be it facilitation or depression, is explained in terms of net loss or gain of exciting or restoring resources. For instance, one mechanism for the monotonic decrease in excitability in a cortical neuron under repetitive stimulation was shown to be an increase in effective potassium membrane conductance [11]. The inverse effect, that is increased excitability, can result from, e.g., the cumulative inactivation of potassium membrane conductance [12]. Such an interplay between opponent processes abounds in models of adaptation.

The selective nature of adaptation is usually interpreted in terms of the spatial locality of the above processes. For instance, [13] showed that constraining the monotonic decrease to a unique subset of synapses allows for selective adaptation of a single neuron to the wide range of inputs received.

A neural correlate of increased sensitivity to the rare, a phenomenon most commonly documented in auditory event related potentials [6], was observed at the level of random networks of cortical neurons *in-vitro* ([14] and [15]), where the mechanism underlying this complex phenomenon is accessible. Using a combination of multi-site recordings, and

pharmacological and electrophysiological manipulations Eytan et al. suggested the following possible mechanism (see schematic illustration in Figure 1): It has been shown in numerous studies that cortical inhibitory interneurons form extended, gap-junction coupled sub-networks [16]. We can hypothesize that such expansive electrically coupled networks are relatively insensitive to the site of stimulation, thus acting as a global component of the system. In contrast, the excitatory population is uncoupled electrically (e.g. [17]) and therefore its activation is pathway specific and is affected locally by stimulation. When one site in the network is stimulated frequently, the local excitatory pathways stemming from this source undergo depression which causes a decline in the network's responsiveness to this stimulation. The inhibitory sub-network is also affected by the frequent stimulation, *albeit globally*, and undergoes depression. The net result is less resistance to the activation pathways stemming from other stimulation sites, hence the enhanced responsiveness to other, less frequently stimulated sites. To support this explanation, Eytan et al. demonstrated that blocking the inhibitory sub-network (by using the GABA antagonist Bicuculline) abolished the increase in the sensitivity to rare stimulation.

Figure 1 about here

In what follows, we formulate a generic mathematical model for the full range of adaptation phenomena, that is: (i) Monotonic facilitation or depression of responsiveness; (ii) Selectivity of adaptation, and (iii) Increased sensitivity to rare stimuli. The model consists of two non linear differential equations, describing the effect of stimulation on the system's exciting and restoring resources. These equations are coupled via functions describing the activities of the two components of the system. This approach enables us to reduce the spatial structure of the system (i.e. globality vs. locality of its different components) into simple, input-output relationships.

To demonstrate its generic nature, the model was applied to two distinctly different systems. First, we develop the equations for transiently responding neural networks. The behavior of such networks is characterized by low tonic activity with reverberating transient responses to stimulation. After formalizing and analyzing this model, we proceed by verifying it using computer simulations and multi-site recordings of large random networks of cortical neurons developing *in-vitro*. Second, we analyze a generic system of coupled populations which maintains a high level of tonic activity in response to steady external stimulation.

Our main contributions in this work are the development of a methodology which facilitates a formal analysis of structurally complex and heterogeneous networks, and the implementation of this methodology to investigate adaptation processes in neural systems. We expect this framework to be applicable to other biological systems as well.

Results

Activity dependent resources model

We consider a system consisting of two components, one excitatory and one inhibitory. The availability of these components is use-dependent, so that the activity of each component results in a decline in its resources. The replenishment process of each resource is assumed to follow first order dynamics with a characteristic time constant. Formally, this can be written

$$(1) \quad \frac{dx_E}{dt} = \frac{1-x_E}{\tau_E} - x_E \tilde{E}(x_E, x_I; s) \quad ; \quad \frac{dx_I}{dt} = \frac{1-x_I}{\tau_I} - x_I \tilde{I}(x_E, x_I; s),$$

where x_E, x_I are the relative availabilities of each resource, τ_E, τ_I are the characteristic time constants and \tilde{E}, \tilde{I} are the activity in each component of the system. We assume here that the activity depends on the state of the system (i.e. resource availabilities) and on external stimulation s .

Now let us assume that the activity in each component has a multiplicative dependence on stimulation intensity, which is a function of one or more parameters of the stimulus (e.g. amplitude, rate, density etc.), namely

$$\tilde{E}(x_E, x_I; s) = s_E E(x_E, x_I) \quad ; \quad \tilde{I}(x_E, x_I; s) = s_I I(x_E, x_I).$$

Here s_E, s_I are the effective intensities of stimulation of each component. By this we assume that each component may be affected differently by each stimulation source, or that it may be affected by a different number of sources. (1) can therefore be rewritten

$$(2) \quad \frac{dx_E}{dt} = \frac{1-x_E}{\tau_E} - x_E s_E E(x_E, x_I) \quad ; \quad \frac{dx_I}{dt} = \frac{1-x_I}{\tau_I} - x_I s_I I(x_E, x_I).$$

We define the system's responsiveness as the excitatory activity, normalized to its non-adapted value

$$(3) \quad R \triangleq \frac{E(x_E, x_I)}{E(1,1)}.$$

By this we assume that most activity in experimental recordings results from the excitatory cells. Since (3) does not depend explicitly on input intensity (see the examples below), the responsiveness can be viewed as the site's normalized input-output gain.

At this stage we do not specify the exact activity functions E and I . However, we can make several reasonable assumptions:

1. Inhibitory activity is explicitly dependent on excitatory activity,

$$(4) \quad I(x_E, x_I) = g(x_E, x_I)E(x_E, x_I).$$

This non-restrictive assumption holds whenever the inhibitory population is not driven directly by external stimulation (see for example the tonic system discussed below).

2. Increasing the excitatory synaptic availability, x_E , increases the excitatory activity, i.e. the responsiveness is a monotonically non-decreasing function of x_E ,

$$(5) \quad \frac{\partial E(x_E, x_I)}{\partial x_E} \geq 0.$$

3. Increasing the inhibitory synaptic availability, x_I , decreases the excitatory activity, i.e. the responsiveness is a monotonically non-increasing function of x_I ,

$$(6) \quad \frac{\partial E(x_E, x_I)}{\partial x_I} \leq 0.$$

Assumptions (5) and (6) refer only to the excitatory activity due to our definition of the system's responsiveness in (3).

In what follows we analyze the system (2), using the above assumptions, in two qualitatively different instances. First, we consider the case of a network with transient responses, to which a periodic stimulation is applied. The results are then compared with experiments in neural networks developing *in-vitro*. Second, we analyze a general network with tonic activity, to which a constant stimulus is applied.

Model network with transient response

The detailed derivation of equation (2) for a transiently responding network, which we used as a reference case, is described in Materials and Methods. In that particular application the stimulation is periodic with an intensity that depends on its period,. Thus, (2) for such systems can written

$$(7) \quad \frac{d\bar{x}_E}{dt} = \frac{1 - \bar{x}_E}{\tau_E} - \bar{x}_E U_E f_E E(\bar{x}_E, \bar{x}_I) \quad ; \quad \frac{d\bar{x}_I}{dt} = \frac{1 - \bar{x}_I}{\tau_I} - \bar{x}_I U_I f_I I(\bar{x}_E, \bar{x}_I) ,$$

where \bar{x}_E, \bar{x}_I are the time-averaged synaptic availabilities, U_E, U_I the synaptic vesicle release probabilities and $f_E = 1/T_E$ and $f_I = 1/T_I$ are the stimulation rates (see Materials and Methods for a derivation, including an explanation for the appearance of the temporal averages). If there are several sources of stimulation in the system, f_E and f_I can express the total or *effective* rate of stimulation influencing each population.

The system described by (2) converges to fixed points in the (\bar{x}_E, \bar{x}_I) plane (referred to as the phase plane), i.e. the loci at which both derivatives vanish. For simplicity, we assume throughout the analysis of this system a linear relationship between the activity functions

$$(8) \quad I(\bar{x}_E, \bar{x}_I) = \alpha E(\bar{x}_E, \bar{x}_I), \quad \alpha > 0$$

In this case, all the fixed points are located along the curve

$$(9) \quad \bar{x}_I^* = \frac{\rho \bar{x}_E^*}{\bar{x}_E^* (\rho - 1) + 1} \quad \text{where} \quad \rho \triangleq \frac{U_E \tau_E f_E}{\alpha U_I \tau_I f_I}$$

(see Materials and Methods) as illustrated in Figure 2. The parameter ρ expresses the ratio between the net effect of stimulation on the excitatory population to its effect on the inhibitory population; e.g. if ρ is larger than one the excitatory population will suffer more resource depletion than the inhibitory one. Alternatively, when $\rho < 1$, the fixed points are all below the diagonal of the phase plane, where inhibition is more depressed than excitation. Thus ρ determines the geometric curve upon which the fixed point is located. The exact location of the fixed point along these curves is determined by the specific parameter values and activity functions.

Figure 2 about here

Frequency dependent adaptation in a transiently responding network

It was shown in [14] that periodic stimulation leads to a decline in the response to each stimulus. Furthermore, this adaptation process becomes more pronounced as the stimulation frequency is increased. In our model, this corresponds to

$$(10) \quad \frac{dR^*}{df_{stim}} < 0,$$

where f_{stim} is the stimulation frequency and the asterisk denotes the steady state value. We will refer to this phenomenon as 'frequency dependent adaptation'. Describing this rather trivial phenomenon will serve as a simple case study which will aid us in understanding the model's behavior.

For the purpose of analytic tractability, let us consider a much simplified symmetric model in which

$$(11) \quad U_E = U_I ; \tau_E = \tau_I ; E \equiv I ; f_E = f_I = f_{stim}.$$

In this case $\rho = 1$ and all fixed points are on the diagonal $\bar{x}_E^* = \bar{x}_I^* = \bar{x}^*$. It is easy to see from (7) that at extremely low stimulation frequency the system converges close to $(\bar{x}_E, \bar{x}_I) = (1, 1)$ where synaptic availabilities are maximal. As the frequency is increased the fixed point shifts along the diagonal towards the origin $(\bar{x}_E, \bar{x}_I) = (0, 0)$ where synaptic depletion is maximal. Therefore, any activity function E which monotonically increases on the diagonal will satisfy (10) and exhibit frequency dependent adaptation. Furthermore, such a function also guarantees the fixed point's stability (see Material and Methods, equation (27)). This can be easily understood intuitively since an increasing activity function creates a negative feedback loop between activity and synaptic availability, which results in a stable steady state solution.

Consider an example of a two-variable sigmoidal function

$$(12) \quad E(\bar{x}_E, \bar{x}_I) = \frac{1}{1 + \exp(-a\bar{x}_E + b\bar{x}_I + \theta)}.$$

It is easy to verify that if $0 < b < a$ then indeed on the diagonal

$$\frac{d}{d\bar{x}} E(\bar{x}, \bar{x}) \geq 0 \text{ for all } \bar{x}.$$

That is to say, when activity depends more strongly on the availability of excitation than on that of inhibition, frequency dependent adaptation will be manifested. This is illustrated in Figure 3.

Figure 3 about here

Selective adaptation in transiently responding networks

Next, we consider the two site stimulation protocol studied in [14], where it was demonstrated experimentally that when one site is stimulated frequently and another site is stimulated rarely, the system reduces its response to the frequent stimulus while enhancing its response to the rare one. It was suggested in [14] that the topological differences between the excitatory and inhibitory subnetworks, and specifically the interconnections within the inhibitory population (e.g. [18]) underlie this phenomenon, whereby the inhibitory population acts as a global common resource affected by stimuli from all sites, while the excitatory network is affected mainly by local stimuli.

Under these assumptions the excitatory populations corresponding to the two sites do not influence each other directly and function as two separate components. The inhibitory population, however, is common (see diagram in Figure 1) and therefore responds to **both**

stimulation sites. In our model, we can easily realize this mechanism by postulating the existence of two excitatory populations and writing the state equations (7) for each stimulation site. Thus, the response to the rarely stimulated site will be according to

$$f_E = f_{rare} \quad ; \quad f_I = f_{freq} + f_{rare} = f_{stim} ,$$

while at the frequent site

$$f_E = f_{freq} \quad ; \quad f_I = f_{freq} + f_{rare} = f_{stim} ,$$

where f_{stim} is the total stimulation intensity applied to the system. Thus the parameter ratio ρ of equation (9) is different at each site

$$\rho_{rare} = \frac{U_E \tau_E f_{rare}}{U_I \tau_I \alpha (f_{freq} + f_{rare})} = \rho_0 \beta \quad ; \quad \rho_{freq} = \frac{U_E \tau_E f_{freq}}{U_I \tau_I \alpha (f_{freq} + f_{rare})} = \rho_0 (1 - \beta) ,$$

with

$$\rho_0 = \frac{U_E \tau_E}{U_I \tau_I \alpha} \quad ; \quad \beta = \frac{f_{rare}}{f_{stim}} = \frac{1}{1 + f_{freq}/f_{rare}} .$$

ρ_0 is the stimuli-independent parameter ratio and β is the normalized intensity of the rare stimulation site ($0 \leq \beta \leq 0.5$). Since $\rho_{rare} < \rho_{freq}$, the adaptation behavior of the rare site will differ from that of the frequent site.

We now define two functionality criteria for this paradigm. 'Selectivity' is defined to be the ratio between the steady state responsiveness at the two sites,

$$(13) \quad S \triangleq \frac{R_{rare}^*}{R_{freq}^*} .$$

'Amplification' is defined to be the steady state increase in the system's sensitivity to the rare stimuli,

$$(14) \quad A \triangleq \frac{E_{rare}^*}{E(1,1)} = R_{rare}^*$$

The dependence of S and A on both the relative intensity β and on the total intensity f_{stim} , for the sigmoidal activity function in (12) is displayed in Figure 4, demonstrating the phenomenon of selective adaptation. The model predicts that selectivity increases with frequency, and that this increase is more pronounced for smaller values of β , i.e. when there is a large difference between the stimulation effect on the two subnetworks. The same holds for the amplification criterion, only that for large values of β no amplification occurs at all (i.e. $A < 1$).

Figure 4 about here

So far, we have developed an averaged model consisting of a single equation for each synaptic population. Using the linear relationship assumption in (8) we located the fixed point of this system on the geometric curves described in (9). At low stimulation rates, all these curves converge to $(\bar{x}_E, \bar{x}_I) = (1, 1)$. As the rates are increased, the curves diverge and the equilibrium location depends more strongly on the relative intensity β . Since the fixed point's location determines the system's responsiveness, assuming integrated activity to be monotonically dependent on resource availability ((5) and (6)) leads to the above predictions for dual site stimulation. Note that at high rates of stimulation ($\sim 100 \text{ sec}^{-1}$) the curves converge towards the origin, where the responsiveness to both sites is extremely low. Since such high stimulation rates are not physiologically possible in *in-vitro* networks, this region does not appear in our analysis. Although we used sigmoidal activity functions for the visualization of these predictions (presented in Figure 4), any activity function obeying (4), (5) and (6) will exhibit the same behavior.

In summary, the theoretical model we have presented so far explains selective adaptation in terms of the change in the availability of the activity dependent resources of the system. The model predicts that selectivity (i.e. the ability of the system to distinguish between different sources) and amplification (i.e. the system's capability to increase its responsiveness to rare events) both depend on stimulation intensity and on the difference between the stimulation sources.

Transiently responding networks - simulation results

A network of leaky integrate-and-fire (LIF) elements was simulated in order to demonstrate the validity of our approach and averaging procedures. It is not meant to provide a comprehensive simulation study of the phenomena. The simulation parameters and setup are detailed in Materials and Methods. Note that all excitatory and inhibitory parameters, as well as the distribution of synapses for all neurons are equal so that the network realizes the symmetrical case in (11). Computing E, I for various values of \bar{x}_E, \bar{x}_I verified that they are indeed similar (data not shown).

Figure 5 depicts the network dynamics for single site stimulation. Panel A shows both excitatory and inhibitory activity during a single transient response. Panel B shows the decrease in normalized network responsiveness towards the steady state level. Panel C and D illustrate the

dynamics of the excitatory and inhibitory depression variables, respectively, and compares their values with those predicted by the averaged equations.

Figure 5 about here

Single site stimulation was repeated for various stimulation frequencies, as shown in Figure 6. Average steady-state values of \bar{x}_E^* , \bar{x}_I^* and their predicted values \bar{x}_E^{*p} , \bar{x}_I^{*p} , calculated from the network's activity using (7), were computed so that the averaging procedure is validated for the entire frequency range (A and B). These values, presented in the phase plane, follow closely the fixed-point loci for $\rho = 1$ depicted in Figure 2 (C). The experimental phenomenon of reduced responsiveness is reconstructed in D.

Figure 7 depicts the dynamics for a dual site stimulation paradigm. Stimuli were delivered either to site 1 (frequent) or to site 2 (rare) every 2 seconds ($f_{stim} = 0.5 \text{ sec}^{-1}$), and the ratio between the stimulation intervals of the two sites was set to be 4:1, which corresponds to $\beta = 0.2$. Panel A depicts the network's dynamics for both sites, while panels B, C and D display the state variable dynamics for site 1 and site 2 local excitatory populations and for the global inhibitory population respectively.

Figure 6, Figure 7 about here

Performing dual-site stimulation on different networks with different values of f_{stim} and β , allowed us to measure the selectivity and amplification variables, as defined in (13) and (14) (Figure 8). The fixed point loci, as predicted in Figure 2, were illustrated by computing the average state variables.

Figure 8 about here

Experimental results

To finally corroborate our model, we performed adaptation experiments in networks of cortical neurons cultured *in-vitro*. The results are presented in Figure 9. Panel A shows frequency dependent adaptation results from 19 networks, stimulated at a single site at various frequencies. Each marker represents the steady state responsiveness (i.e. the total number of

spikes observed in the network within 150msec after a stimulus), normalized to the initial response of each network. A marked decline in responsiveness appears for rates larger than 0.1 sec^{-1} , while the networks fail to respond steadily when stimulated above 0.5 sec^{-1} .

Next, a network was stimulated at two sites ($\sim 1\text{mm}$ apart) following the paradigm in [14], using different stimulation rates ($1/3 \text{ sec}^{-1}$ and $1/5 \text{ sec}^{-1}$) and ratios (1:1, 1:4 and 1:9, $\beta=0.5, 0.2$ and 0.1 respectively). Thus we obtained 6 measurements from which we computed selectivity (Figure 9B) and amplification (Figure 9C) for each scenario according to (13) and (14). Comparing these results with those presented in Figure 4 and Figure 8 we can conclude that for high stimulation ratios ($\beta=0.1$), both selectivity and amplification exhibit the expected frequency dependence. At lower ratios, however, selectivity decreases as frequency is increased, which means that the site chosen for rare stimulation undergoes more pronounced depression. In terms of our model, this means that when stimulation frequencies are identical $\beta > 0.5$ for this choice of stimulation sites.

Figure 9 about here

A network model with tonic activity

So far we have applied our approach to systems with transient, phasic response to external stimulation and a low level of tonic activity. To demonstrate our approach in another, qualitatively different system, we now consider a Wilson-Cowan [19] type system, consisting of excitatory and inhibitory components,

$$(15) \quad \begin{aligned} \tau_1 \frac{de}{dt} &= -e + [F_e + w_{ee}e - w_{ei}i]_+ \\ \tau_2 \frac{di}{dt} &= -i + [F_i + w_{ie}e - w_{ii}i]_+ \end{aligned}$$

where τ_1 and τ_2 are the characteristic time constants, e and i the activities and F_e and F_i the feedforward stimulation intensities of the excitatory and inhibitory components. The components' interactions are mediated by the non-negative synaptic weights w_{ij} . The '+' subscripts indicate that negative terms are clipped to zero. Such schematic systems have been used in many theoretical studies (see, for example, [20] section 7.5).

To apply our model for selective adaptation to this system, we assume that the external drive to the inhibitory population is negligible (compared with the excitatory and recurrent drive to this

population), namely $F_i \cong 0$. The system with this additional assumption is illustrated in Figure 10.

Figure 10 about here

Now let us assume that the synaptic efficacies are subject to depression processes,

$$(16) \quad w_{ee} = x_E W_{ee} \quad ; \quad w_{ei} = x_I W_{ei} \quad ; \quad w_{ie} = x_E W_{ie} \quad ; \quad w_{ii} = x_I W_{ii},$$

where W_{ij} are the maximal synaptic efficacies and x_E and x_I are the relative resource availabilities, which follow the dynamics of equation (2). We also assume that the neural activity time constants τ_1 and τ_2 are much shorter than the synaptic availability time constants τ_E and τ_I , so that activities reach their steady state values instantaneously. Defining

$$E(x_E, x_I) \triangleq \frac{1 + x_I W_{ii}}{1 + x_E x_I (W_{ei} W_{ie} - W_{ii} W_{ee}) + x_I W_{ii} - x_E W_{ee}},$$

$$I(x_E, x_I) \triangleq \frac{x_E W_{ie}}{1 + x_E x_I (W_{ei} W_{ie} - W_{ii} W_{ee}) + x_I W_{ii} - x_E W_{ee}},$$

the steady state solution of (15) is given by

$$(17) \quad \tilde{E} = E(x_E, x_I) F_e$$

$$\tilde{I} = I(x_E, x_I) F_e = \frac{x_E W_{ie}}{1 + x_I W_{ii}} \tilde{E}.$$

As can be seen the steady state activities have a multiplicative dependency on external stimulation intensity, as required by our model. Local stability of the solution given in (17), ensuring convergence to a fixed point, is guaranteed for all x_E, x_I if $W_{ee} < 1$ (see Materials and Methods). Unstable solutions, where the system develops oscillatory activity, will not be discussed here.

Next we check the system's compliance with assumption (4),(5) and (6). Assumption (4), namely the explicit dependence of the inhibitory activity on the excitatory activity is readily seen in (17). Note that this dependence differs from the proportionality assumed in (8), in that the ratio I/E (i.e. the function $g(x_E, x_I)$ in (4)) is no longer constant. This difference between the two systems changes the phase plane structure but not the qualitative behavior, as discussed below. Differentiating with respect to the excitatory resource availability we have

$$\frac{\partial E}{\partial x_E} = \frac{W_{ee} - (W_{ei} W_{ie} - W_{ee} W_{ii}) x_I}{1 + W_{ii} x_I} E^2,$$

and therefore the monotonicity condition (5) is satisfied in this system when

$$W_{ee} > \frac{W_{ei} W_{ie}}{1 + W_{ii}}.$$

Differentiating with respect to the inhibitory resource availability we have

$$\frac{\partial E}{\partial x_I} = -\frac{x_E W_{ei} W_{ie}}{(1 + x_I W_{ii})^2} E^2 \leq 0$$

And therefore condition (6) is indeed satisfied for all x_E, x_I .

The fixed points of the system are located on curves in the phase plane,

$$(18) \quad x_E^* = 1 - \frac{(1 + W_{ii} x_I^*)(1 - x_I^*)}{x_I^*} \rho \quad \text{where} \quad \rho \triangleq \frac{U_E \tau_E F_E}{W_{ie} U_I \tau_I F_I}.$$

F_I is the stimulation intensity affecting the inhibitory population indirectly through the excitatory drive to it, and may differ from F_E when two stimulation sources are present, as explained below. The curves, presented for different values of ρ in Figure 11, differ from those in the transient response system due to the different dependence described above. However, as x_E^* and x_I^* approach unity this difference vanishes. Moreover, in what follows we demonstrate that the qualitative nature of selective adaptation is maintained in this system. (18) can be simplified assuming $W_{ii} \ll 1$, in which case we get

$$(19) \quad x_I^* = \frac{\rho}{1 + \rho - x_E^*}$$

with ρ defined as in (18). In fact, the curves in (18) and in (19) are similar even when W_{ii} approaches unity.

Figure 11 about here

Selective adaptation in networks with tonic activity

We now consider the two site stimulation scenario for this system. The model for this system is presented in Figure 12, resembling our conceptual model in Figure 1. The inhibitory population is global and therefore is driven by both excitatory populations. In the tonic system, however, instead of rare and frequent stimulation sites we have 'strong' and 'weak' sites. The responses at these two sites are

$$\begin{aligned} \rho_{weak} &= \frac{U_E \tau_E F_{weak}}{U_I \tau_I W_{ie} F_{stim}} = \rho_0 \beta \\ \rho_{str} &= \frac{U_E \tau_E F_{str}}{U_I \tau_I W_{ie} F_{stim}} = \rho_0 (1 - \beta) \\ \rho_0 &= \frac{U_E \tau_E}{U_I \tau_I W_{ie}} \quad ; \quad F_{stim} = F_{weak} + F_{str} \quad ; \quad \beta = \frac{F_{weak}}{F_{stim}} = \frac{1}{1 + F_{weak}/F_{str}} \end{aligned}$$

We define selectivity and amplification in this system using (3), (13) and (14). The dependence of these measures on total and relative stimulation intensities, F_{stim} and β , is presented in Figure 12. The figures are sketched in logarithmic scale so two regions of behavior appear. At low intensity of stimulation (low F_{stim}), where both sites are highly responsive, selectivity is monotonically increasing with input intensity. At high intensity of stimulation (high F_{stim}) the system's responsiveness becomes very low and therefore selectivity and amplification decline. As mentioned above, such behavior was also observed outside the physiological bounds in the transiently responding network model (data not shown).

Figure 12 about here

Discussion

In this work we have formalized a model describing the various adaptation phenomena in neural populations. In many studies, adaptation was modeled in terms of cumulative effects of stimulation on either the exciting or the restoring resources of the system. These changes in resource availability lead to either a decrease or an increase in the system's responsiveness. When spatial segregation between the stimulation pathways is introduced, the effect of stimulation on the resources is local. Such a system will exhibit selective adaptation, the ability to adapt to one source while preserving its sensitivity to another. Far less trivial is the phenomenon we term 'amplification', which is an increased sensitivity to rare stimulation on the background of frequent stimulation. This phenomenon characterizes the MMN evoked potential and was also observed *in-vitro*.

The ability of a network to perform selective adaptation has obvious functional implications. Applied as a filter in a sensory information pathway, for instance, this system can implement novelty detection, enhancing the propagation of rare sensory events while attenuating frequent events. Selective adaptation is one of the few phenomena observed in neural networks developing *in-vitro* that has a well understood, non-trivial biological function. As such, it can serve as a benchmark to assess the functional complexity of such networks.

We developed a simple model describing the effect of external stimulation on each component of the system. This model was implemented on two types of neural systems, the first characterized by a transient response and the second by a tonic response. The model suggests that non-trivial adaptation phenomena can arise in a system with a relatively simple structure. The key requirement from the model is that the restoring resource (i.e. the inhibitory component) is affected globally from all stimulation pathways.

To test our model, we observed the dependence of both the system's selectivity and amplification on stimulation intensity, and on the ratio between intensities at two stimulation sites. For the transient responses network, the model predicts that within the physiological bounds (i) selectivity increases as stimulation frequency is increased, (ii) this sensitivity is more pronounced as the ratio between frequencies of rare and frequent stimuli increases and (iii) amplification is also frequency dependent, but can only occur at high ratios, i.e. when the

stimulation rates are very different. These predictions were compared with computer simulations and with data from recordings in neural cultures developing *in-vitro*.

In addition to predicting novel phenomena, our mathematical formalization provides further insight into adaptation processes. One clear benefit of a mathematical formalization involves the reduction of several variables to a single variable, which suffices to fully describe the behavior of interest, akin to an order parameter in Physics. For instance, it has been reported in several studies that synaptic depression parameters differ between excitatory and inhibitory neurons [21]. This asymmetry in adaptive behavior formed the basis of a recent theoretical study [22]. According to our model, all the stimuli-independent physiological constants are reduced to a single ratio ρ_0 which determines the system's steady state behavior. Finally, a distinct benefit of our formal description is the ability it provides to generalize from our specific experimental system to new systems, sharing its basic characteristics, such as the tonic activity system presented in this paper.

As mentioned above, one of our main assumptions is that the inhibitory population serves as a global component in the system. We implemented this assumption in our model by separating the excitatory population into two segregated networks, both connected to a common inhibitory population. This was also the design we used for the leaky integrate-and-fire neural network simulation. Admittedly, this structure is a limiting case for our assumptions on the sub-networks' topologies, as one might expect that a more realistic network will include some interactions between the two excitatory sites and some degree of locality in the inhibitory one. In such a network the stimulation sites are not as distinct and therefore are affected more similarly by the stimuli. In other words β will be closer to 0.5, where the response to the two inputs is identical. In that sense β , which in our 'extremist' model relates only to the difference between the inputs, may also represent the differences in component structure.

Another key assumption used in the development of our model is that the system has separable time scales; a fast time scale governing short term transients (e.g. membrane voltage, fast depression and facilitation) and a slow time scale (e.g. slow synaptic depression). This separation enabled us to extract the 'slow evolution' of the system's state variables, either by using averaging methods (as was done in the transiently responding network example) or by assuming instantaneous response (as was done in the tonically firing network example). One

must note that all information conveyed in the fast dynamics of the system (e.g. latency, pattern of firing etc.) is ignored using this technique.

In this work we have dealt with systems receiving input from one or two sources. An appealing possibility for future work is to broaden the model to systems receiving input from a continuum of input sources. For instance, an auditory cortical column responds to a range of stimulation frequencies. We hypothesize that the correlate of selective adaptation in such systems, the so called 'repulsive shifts' in their tuning curves (e.g. [8], [22]), may arise from differences in the connectivity of the inhibitory and excitatory populations composing these systems. A model of such systems can also include more realistic connectivity schemes, as discussed above.

It is noteworthy that an essential component of our model is the globality of the inhibitory network, owing mostly to the electrical interconnections of this population via gap junctions (see [16-18]). This offers a compelling role to the abundance of connexins in the inhibitory neurons of the neocortex (e.g. [23]). A straightforward prediction of this hypothesis, then, is the abolishment of amplification in the absence of functional gap-junctions. An experiment verifying this prediction is yet to be performed.

To summarize, in this contribution we have developed a methodology which enabled us to reduce complex, heterogeneous networks to a minimal set of state equations. This procedure was implemented in order to investigate adaptation processes, which are vital features of biological systems in general, and neural networks in particular.

Materials and Methods

Derivation of state equations for transiently responding neural networks

We consider a network composed of excitatory and inhibitory neurons with a very low level of intrinsic (spontaneous) activity. The network responds to a short (less than 1msec) external stimulus in a reverberating episode of increased activity (several tens of msec) which we will refer to as the transient response (TR, sometimes referred to as 'Network Spikes' or 'Bursts', see [24-27]). Unlike a stereotypical action potential of single neurons, however, this response is graded, namely the magnitude of each response varies and depends on the current state of the system. When stimulated repeatedly, the system's response was shown to decrease monotonically with stimulation frequency ([14,15,28]). It was suggested that this decrease depends heavily on a decline in synaptic availability [29]. Based on these observations, we formulate below a model in which synaptic resource availabilities play the role of state variables.

We consider two populations of synapses, where each synapse (inhibitory or excitatory) is subject to short term plasticity modeled by a differential equation [30]

$$\frac{dx_j}{dt} = \frac{1-x_j}{\tau_j} - U_j x_j \sum_{t_{sp}} \delta(t-t_{sp}),$$

where x_j represents the relative availability of release-ready synaptic vesicles, $\{t_{sp}\}$ denotes the times of firing by the pre-synaptic neuron; synaptic parameters are τ_j (recovery time constant) and U_j (the fraction of vesicles released for each pre-synaptic action potential). Between firing times t_n and t_{n+1} , the synapse recovers exponentially towards 1,

$$x_j(t) = (x_j(t_n) - 1) \exp\left(-\frac{t-t_n}{\tau_j}\right) + 1, \quad t_n \leq t < t_{n+1},$$

while upon the arrival of a pre-synaptic spike at time t_n , the synapse utilizes a fraction of its resource (i.e. releases a fraction of the available vesicles)

$$x_j(t_n^+) = (1 - U_j) x_j(t_n^-),$$

where t_n^-/t_n^+ denote the time immediately before/after the n -th spike. We note that this equation guarantees that x_j remains in the range 0-1.

Typically in mean field analysis of neural ensembles, one assumes that individual neurons fire as non-homogeneous Poisson processes and are sparsely connected to each other. Since the

present analysis focuses on synaptic ensembles rather than neural ensembles, and since all synapses sharing the same pre-synaptic neuron receive the same input, these assumptions do not hold. However, if we assume that the total number of synapses in the network is much larger than the number of synapses per neuron and that connectivity is approximately uniform, we can neglect these inter-synaptic correlations (similarly to [30]). We can then average over the ensemble of synapses to get the mean population behavior

$$(20) \quad \frac{dx_E}{dt} = \frac{1-x_E}{\tau_E} - U_E x_E \tilde{E}(t) \quad ; \quad \frac{dx_I}{dt} = \frac{1-x_I}{\tau_I} - U_I x_I \tilde{I}(t),$$

where x_E, x_I are the average available synaptic resources for the excitatory and inhibitory populations, respectively. The average activity rates in these populations, \tilde{E} and \tilde{I} , depend on the available synaptic resources but vary with time as a result of 'fast' processes and external stimulation.

Now let us assume that each population (excitatory and inhibitory) is stimulated periodically with period T_E or T_I and responds to each stimulus with a short transient response (TR). Since we are interested in the cumulative effect of stimulation on the network, we average each equation over a single period of stimulation

$$\bar{x}_E \triangleq \frac{1}{T_E} \int_{T_E} x_E(t) dt \quad ; \quad \bar{x}_I \triangleq \frac{1}{T_I} \int_{T_I} x_I(t) dt.$$

We can take the state variables to be relatively constant during a single response, which simplifies the integration

$$(21) \quad \frac{d\bar{x}_E}{dt} = \frac{1-\bar{x}_E}{\tau_E} - U_E \bar{x}_E \frac{1}{T_E} \int_{T_E} \tilde{E}(t) dt \quad ; \quad \frac{d\bar{x}_I}{dt} = \frac{1-\bar{x}_I}{\tau_I} - U_I \bar{x}_I \frac{1}{T_I} \int_{T_I} \tilde{I}(t) dt.$$

When the duration of the transient response T_{TR} is much shorter than the stimulation periods T_E and T_I , the integration is independent of these periods. Furthermore, the outcome of this integration depends only on the synaptic availabilities at the stimulus onset. We define the populations' integrated 'activity functions' as

$$E(\bar{x}_E, \bar{x}_I) \triangleq \int_{T_{TR}} \tilde{E}(t) dt \quad ; \quad I(\bar{x}_E, \bar{x}_I) \triangleq \int_{T_{TR}} \tilde{I}(t) dt.$$

Substituting these definitions in (21) we obtain the averaged state equations

$$(22) \quad \frac{d\bar{x}_E}{dt} = \frac{1-\bar{x}_E}{\tau_E} - U_E f_E \bar{x}_E E(\bar{x}_E, \bar{x}_I) \quad ; \quad \frac{d\bar{x}_I}{dt} = \frac{1-\bar{x}_I}{\tau_I} - U_I f_I \bar{x}_I I(\bar{x}_E, \bar{x}_I),$$

where $f_E = 1/T_E$ and $f_I = 1/T_I$ are the stimulation rates.

Fixed point location

The fixed points of the averaged system (22) are located where both derivatives vanish, namely

$$(23) \quad \frac{1-\bar{x}_E^*}{\tau_E} - U_E f_E \bar{x}_E^* E(\bar{x}_E^*, \bar{x}_I^*) = 0 \quad ; \quad \frac{1-\bar{x}_I^*}{\tau_I} - U_I f_I \bar{x}_I^* I(\bar{x}_E^*, \bar{x}_I^*) = 0.$$

Dividing the first equation by the second one we get

$$\frac{1-\bar{x}_E^*}{1-\bar{x}_I^*} = \frac{U_E \tau_E f_E \bar{x}_E^* E(\bar{x}_E^*, \bar{x}_I^*)}{U_I \tau_I f_I \bar{x}_I^* I(\bar{x}_E^*, \bar{x}_I^*)}.$$

We can reasonably assume that

$$(24) \quad I(\bar{x}_E, \bar{x}_I) = g(\bar{x}_E, \bar{x}_I) E(\bar{x}_E, \bar{x}_I),$$

where g is some function of the resource availabilities (this relationship is plausible when the inhibitory population is not driven by external sources, e.g. in the tonic system discussed above).

Let us consider the simple case where $I(\bar{x}_E, \bar{x}_I) = \alpha E(\bar{x}_E, \bar{x}_I)$ with $\alpha > 0$. The fixed point equation under this assumption reduces to

$$\frac{1-\bar{x}_E^*}{1-\bar{x}_I^*} = \rho \frac{\bar{x}_E^*}{\bar{x}_I^*}$$

$$\bar{x}_I^* = \frac{\rho \bar{x}_E^*}{\bar{x}_E^* (\rho - 1) + 1}; \quad \rho = \frac{U_E \tau_E f_E}{U_I \tau_I f_I \alpha}.$$

Therefore, the parameter ratio ρ determines the geometric locus (curve) of the system's fixed points. The exact location of the fixed point on this curve is governed by the specific parameter values and activity functions E, I .

Stability analysis

The asymptotic stability of the system's fixed point is determined by the eigen values of the Jacobian matrix at these points

$$J(\bar{x}_E^*, \bar{x}_I^*) = \begin{pmatrix} \partial_{\bar{x}_E} \dot{\bar{x}}_E & \partial_{\bar{x}_I} \dot{\bar{x}}_E \\ \partial_{\bar{x}_E} \dot{\bar{x}}_I & \partial_{\bar{x}_I} \dot{\bar{x}}_I \end{pmatrix} \Bigg|_{(\bar{x}_E^*, \bar{x}_I^*)}$$

$$= \begin{pmatrix} -1/\tau_E - U_E f_E (E + \bar{x}_E \partial_{\bar{x}_E} E) & -U_E f_E \bar{x}_E \partial_{\bar{x}_I} E \\ -U_I f_I \bar{x}_I \partial_{\bar{x}_E} I & -1/\tau_I - U_I f_I (I + \bar{x}_I \partial_{\bar{x}_I} I) \end{pmatrix} \Bigg|_{(\bar{x}_E^*, \bar{x}_I^*)},$$

where ∂_x denote partial derivation with respect to x . Necessary and sufficient conditions for stability are (see [31], section 5.2):

$$(25) \quad \text{i.} \quad T = \text{trace}\{J\} < 0,$$

$$\text{ii. } D = \det\{J\} > 0.$$

We consider the simple case of a symmetric system in which

$$U_E = U_I; \tau_E = \tau_I; f_E = f_I; E \equiv I.$$

In this system $\rho = 1$ so that the fixed points are at $\bar{x}_E^* = \bar{x}_I^* = \bar{x}^*$.

Computing the stability criteria (25) for this system yields

$$(26) \quad \left. (\partial_{\bar{x}_E} E + \partial_{\bar{x}_I} E) \right|_{(\bar{x}^*, \bar{x}^*)} > -\frac{E(\bar{x}^*, \bar{x}^*)}{\bar{x}^*(1-\bar{x}^*)}.$$

We note that the activity function's directional derivative along the diagonal $\bar{x}_E^* = \bar{x}_I^* = \bar{x}^*$ (i.e. the derivative along the fixed point loci) is

$$\frac{dE}{d\underline{l}} = \frac{\nabla E \cdot \underline{l}}{|\underline{l}|} = \frac{\partial_{\bar{x}_E} E + \partial_{\bar{x}_I} E}{\sqrt{2}} \quad \underline{l} = (1, 1).$$

Thus, the stability criterion (26) can be rewritten

$$(27) \quad \left. \frac{dE}{d\underline{l}} \right|_{(\bar{x}^*, \bar{x}^*)} > -\frac{E(\bar{x}^*, \bar{x}^*)}{\sqrt{2}\bar{x}^*(1-\bar{x}^*)}.$$

Specifically, if the system's activity depends more strongly on the availability of excitation than on that of inhibition, then its activity increases along the diagonal,

$$\left. \frac{dE}{d\underline{l}} \right|_{(\bar{x}^*, \bar{x}^*)} \geq 0.$$

In this case response is non-increasing with stimulation frequency, (27) is always satisfied and the fixed point is stable. This is easily explained intuitively as a negative feed-back arising between the state variables and the activity.

Stability analysis of the tonic system

Since we assume the neural activity time constants, τ_1 and τ_2 , are much shorter than the synaptic availability time constants τ_E and τ_I , we can analyze the stability of (15) assuming x_E and x_I are fixed, since they change little while e and i change. The Jacobian matrix derived from the system (15) is

$$J = \begin{pmatrix} \partial_e e & \partial_i e \\ \partial_e i & \partial_i i \end{pmatrix} = \begin{pmatrix} \frac{x_E W_{ee} - 1}{\tau_1} & -\frac{x_I W_{ei}}{\tau_1} \\ \frac{x_E W_{ie}}{\tau_2} & -\frac{x_I W_{ii} + 1}{\tau_2} \end{pmatrix},$$

(see stability analysis of (\bar{x}_E, \bar{x}_I) , above). The trace of this matrix is negative when

$$x_E W_{ee} < \frac{\tau_1}{\tau_2} (x_I W_{ii} + 1) + 1,$$

which is fulfilled for all (x_E, x_I) when $W_{ee} < \frac{\tau_1}{\tau_2} + 1$. The determinant is positive under the condition

$$x_E W_{ee} < x_E x_I (W_{ie} W_{ei} - W_{ee} W_{ii}) + x_I W_{ii} + 1,$$

which is fulfilled for all (x_E, x_I) when $W_{ee} < 1$. We conclude that both stability conditions are met when $W_{ee} < 1$.

Simulation

The simulation included a network of leaky integrate and fire equations

$$\frac{dv_j(t)}{dt} = -\frac{v_j(t)}{\tau_m} + \sum_i w_{ji}(t) \sum_f \delta(t - t_i^{(f)} - \Delta_{ji}) + I_j(t) + n_j(t)$$

if $v_j(t) = v_{th}$ set $t_j^{(f)} = t$ and $v_j(t) = v_r$

Each synapse is characterized by its efficacy w_{ji} and delay Δ_{ji} . Two synaptic depression processes were modeled, based on [21] and [32]

$$\frac{dD_j(t)}{dt} = \frac{1 - D_j(t)}{\tau_{Dj}} - U_{Dj} D_j(t) \sum_f \delta(t - t_j^{(f)})$$

$$\frac{dx_j(t)}{dt} = \frac{1 - x_j(t)}{\tau_{xj}} - U_{xj} x_j(t) \sum_f \delta(t - t_j^{(f)})$$

where D_j and x_j are the fast and slow synaptic depression variables respectively. The synaptic efficacy of each neuron is determined by the equation

$$w_{ji}(t) = W_i D_i(t) x_i(t) \quad \text{for all } j.$$

In the single site stimulation paradigm, a network of 100 excitatory neurons and 40 inhibitory neurons was simulated, each driving 12 synapses (connectivity was uniformly random). In the dual site stimulation paradigm, 200 excitatory neurons were separated into two segregated populations, both connected to the 'global' inhibitory population randomly.

Stimuli were applied periodically by injecting a current pulse randomly into 10% of the stimulated neural populations

$$I_j(t) = I \sum_{n=0,1,2,\dots} \delta(t - nT_j),$$

where T_j is the stimulation period.

Each neuron is also subject to random white Gaussian noise

$$n_j(t) \sim \mathcal{N}(0, \sigma_N).$$

Table 1 summarizes the values used for each parameter mentioned in the above description. These were chosen so that the system's time scales resemble those in [14]. In particular, the system is non-responsive to stimulation beyond 0.5 sec^{-1} , and adaptation is significant beyond 0.1 sec^{-1} .

Variable	Value	Comments
τ_m	20ms	Membrane time constant
v_r	0mV	Reset potential
v_{th}	10mV	Threshold potential
τ_D	200ms	Fast depression recovery time constant
U_D	0.3	Fast depression release probability
τ_x	8sec	Slow depression recovery time constant
U_x	0.05	Slow depression release probability
W_E	20	Excitatory synaptic efficacy
W_I	-20	Inhibitory synaptic efficacy
Δ_E	1-4ms (uniformly)	Excitatory synaptic delay
Δ_I	1ms	Inhibitory synaptic delay
I	100mA	Injected current magnitude
σ_N	0.3mA	Noise STD

Table 1: Summary of simulation parameter values

Cultured networks

Cortical neurons were obtained from newborn rats within 24 hr after birth, following standard procedures as described previously [25,33]. The cortical tissue was enzymatically digested and mechanically dissociated. The neurons were plated directly onto substrate-integrated multi-electrode array (MEA) dishes [34]. The cultures were bathed in MEM supplemented with heat inactivated horse serum (5%), glutamine (0.5mM), glucose (20mM), and gentamycin (10 $\mu\text{g/ml}$) and maintained in an atmosphere of 37°C , 5% CO_2 and 95% air in a tissue culture incubator as well as during the recording phases. Experiments were performed during the third week after plating, thus allowing functional and structural maturation of the neurons [33].

Electrophysiology

We used arrays of 60 Ti/Au/TiN electrodes, 30 μ m in diameter and spaced 200 μ m from each other (MultiChannelSystems, Reutlingen, Germany). The insulation layer (silicone nitride) was pretreated with poly-D-lysine. A commercial 60-channel amplifier (B-MEA-1060, MultiChannelSystems) with frequency limits of 1–5000 sec⁻¹ and a gain of 1024X was used. The B-MEA-1060 was connected to MCPPlus variable gain filter amplifiers (Alpha-Omega, Nazareth, Israel) for further amplification. Stimulation through the MEA was performed using a dedicated eight-channel stimulus generator (MultiChannelSystems). Data were digitized using two, parallel 5200a/526 analog-to-digital boards (Microstar Laboratories, Bellevue, WA). Each channel was sampled at a frequency of 24 kilosample/sec and prepared for analysis using the AlphaMap interface (Alpha-Omega). Thresholds (8X rms units, typically in the range of 10–20 μ V) were defined separately for each of the recording channels before the beginning of the experiment. Before each experiment and between stimulation epochs, the networks were monitored for at least 15 min to ensure stability of the activity and to allow recovery.

Selectivity error bounds were defined as

$$(28) \quad S_{\min} = \frac{R_{rare}^* - \overline{SEM}_{rare}}{R_{freq}^* + \overline{SEM}_{freq}}; S_{\max} = \frac{R_{rare}^* + \overline{SEM}_{rare}}{R_{freq}^* - \overline{SEM}_{freq}},$$

where \overline{SEM} is the standard error of mean responsiveness, normalized to the un-adapted response.

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Captions

Figure 1: Diagram of dual site stimulation model

Stimulation effect on the excitatory populations is local, and therefore there is stronger depression of that population at the frequent site. The effect on the inhibitory resource, however, is global due to its interconnectivity so it is affected by stimulation at all sites. Thus, response to the rare site may be increased due to the global decline in inhibition.

Figure 2: Fixed point loci when the activities are proportional

Geometrical loci of the averaged system's fixed points when the excitatory and inhibitory activity function are proportional to each other, as described in (8). The locus depends on the parameter ratio ρ . When $\rho < 1$ fixed points are located in the lower half of the plane ($\bar{x}_E^* > \bar{x}_I^*$) and vice versa. We can infer from the assumptions in (5) and (6) that as fixed points approach the lower-right corner of the phase plane, activity increases. Thus, decreasing ρ changes the overall behavior from a depressing to a facilitating one.

Figure 3: Frequency dependent adaptation in the theoretical symmetric system

State variables and responsiveness decrease monotonically as stimulation frequency is increased. The curve was calculated for the symmetric system satisfying (11) where the system's activity functions are the sigmoidal activity function given in (12) ($a=16.67$; $b=10$; $\theta=5$; $U=0.5$; $\tau=10$ sec).

Figure 4: Selective adaptation in the theoretical model

(A) Selectivity as defined in (13), for a selective adaptation paradigm using the sigmoidal activity function given in (12) (parameter values as in Figure 3). Here we also assume $\rho_0 = 2$. Selectivity is monotonically increasing in f_{stim} and decreasing in β . (B) Amplification as defined in (14), for the same paradigm. For high values of β (here, for $\beta=0.5, 0.4$ and 0.3) amplification is decreasing with stimulation frequency and is below 1 (i.e. the response to the rare is in fact depressed). When β is further decreased (here, for $\beta=0.2$ and 0.1), amplification becomes non-decreasing and above 1 so that the response is indeed amplified. (C) phase plane loci of fixed points for the rare (green) and frequent (blue) sites for different values of β (marked on the curves). Note that for each value of β , $\rho_0 = \rho_{rare} + \rho_{freq}$ so that when the locus curve of the rare shifts towards the lower right corner (i.e. towards amplification) the locus curve of the frequent shifts towards the upper left corner (i.e. towards stronger depression).

Figure 5: Single site stimulation in a simulated network

The simulation model consisted of a network of leaky integrate and fire neurons with depressing synapses, as described in Materials and Methods. (A) The network is stimulated every 3 seconds to produce a transient response of both the inhibitory and the excitatory subnetworks. (B) The network adapts to the stimulus and the total responsiveness (as defined in (3)) declines. (C,D) Comparing the slow depression variables, averaged over the populations, x_E and x_I , and the value predicted from the network's activity, x_E^p and x_I^p (using equation (20), where \tilde{E} and \tilde{I} are the activities obtained from the simulation), validates our assumptions for averaging over neural ensembles. Furthermore, the time-averaged variables \bar{x}_E, \bar{x}_I and their predicted value \bar{x}_E^p, \bar{x}_I^p (calculated from the averaged network's activity using (7), where E and I are the integrated activity obtained from the simulation) converge to a similar steady-state value, which validates our assumptions for averaging over the stimulation period.

Figure 6: Frequency dependent adaptation in simulated networks

10 different networks were stimulated repeatedly at various frequencies ($1/30 \text{ sec}^{-1}$, $1/20 \text{ sec}^{-1}$, $1/15 \text{ sec}^{-1}$, $1/10 \text{ sec}^{-1}$, $1/7 \text{ sec}^{-1}$, $1/5 \text{ sec}^{-1}$, $1/4 \text{ sec}^{-1}$, $1/3 \text{ sec}^{-1}$, $1/2 \text{ sec}^{-1}$) and the results were averaged. (A, B) Steady-state values of the state variables \bar{x}_E^*, \bar{x}_I^* and their predicted values $\bar{x}_E^{*p}, \bar{x}_I^{*p}$ (see Figure 5) were computed from the last 8 cycles of each simulation. (C) The phase plane fixed points are indeed located close to the diagonal of $\rho = 1$, as expected. (D) The last 8 responses from all the networks were averaged to produce the steady state responsiveness of the system.

Figure 7: Dual site stimulation dynamics in simulated networks

(A) Network response to rare (circles) and frequent (squares) stimulation. Stimulation ratio was 4:1 ($\beta=0.2$) at 0.5 sec^{-1} . (B) The average synaptic availability at the frequent site. (C) The average synaptic availability at the rare site. (D) The average synaptic availability at the global inhibitory site.

Figure 8: Selective adaptation in simulated networks

Results are averaged from 10 different random networks. (A,B) Dependence of selectivity (as defined in (13)) and amplification (as defined in (14)) on stimulation frequencies and relative intensity. For frequent-rare ratios greater than one, selectivity increases with stimulation frequency. However, amplification (increased sensitivity to the rare) is pronounced only for high ratios. Both results agree with the theoretical predictions presented in Figure 4. (C) Dependence of the fixed point loci for the frequent (squares) and rare (circles) sites on frequencies and ratios. For a 1:1 ratio ($\beta=0.5$), both sites are identically stimulated and so converge to the same fixed point in the phase plane. As β is decreased, ρ_{rare} decreases while ρ_{freq} increases. The curves were fitted according to (9), values of ρ for each curve were found by trial

and error: for $\beta=0.1$, $\rho_{rare}=0.2$ and $\rho_{freq}=1.45$ (solid lines); for $\beta=0.2$, $\rho_{rare}=0.35$ and $\rho_{freq}=1.1$ (dashed lines); for $\beta=0.5$ $\rho_{rare}=\rho_{freq}=0.75$ (dotted line). Using the identity $\rho_0 = \rho_{rare} + \rho_{freq}$ we can estimate that for this system $\rho_0 \cong 1.5$.

Figure 9: Experimental results from neural cultures developing *in-vitro*

(A) Frequency dependent adaptation. 19 networks were stimulated at different frequencies (0.02-0.5 sec⁻¹). At each frequency the networks were stimulated for 900 seconds, long enough to reach steady state. Responsiveness is defined as the mean number of spikes detected in a network within 150 msec after a stimulus. Steady state responsiveness was computed by averaging over the last 6 responses following repetitive stimulation at a given frequency f_{stim} . The result was normalized to the networks' initial responsiveness to produce R as defined in (3). Error bars mark \pm SEM.

(B,C) Dual site stimulation. Stimuli were applied at two stimulation rates (once every 5 sec and once every 3 sec) and in three patterns: 1:4, 1:9 and 1:1 (sites A and B respectively, i.e. $\beta=0.2, 0,1$ and 0.5 respectively) in a paradigm similar to that described in [14] (total of 6 different stimulation epochs). Responsiveness is defined as the total number of spikes in the network within 150 msec after a stimulus. The network was allowed 15 minutes of recovery between epochs. Panel B shows the dependence of selectivity (as defined in (13)) and panel C that of amplification (as defined in (14)) on stimulation frequencies and ratios. Steady state responsiveness was computed by averaging over all responses to a site in the last half of each epoch. These were normalized to the un-adapted response, defined as the maximal response in the first 30sec of each epoch (this definition was used to overcome rapid transients in the initial response). Error bars in (A) mark S_{min} and S_{max} (see Materials and Methods equation (28)). Error bars in (B) mark \pm SEM (normalized to the un-adapted response).

Figure 10: Model for network with tonic activity

The model consists of two coupled populations, excitatory and inhibitory. We assume the inhibitory population is not driven directly by external stimulation. Each population responds via a threshold linear response function, as described in (15).

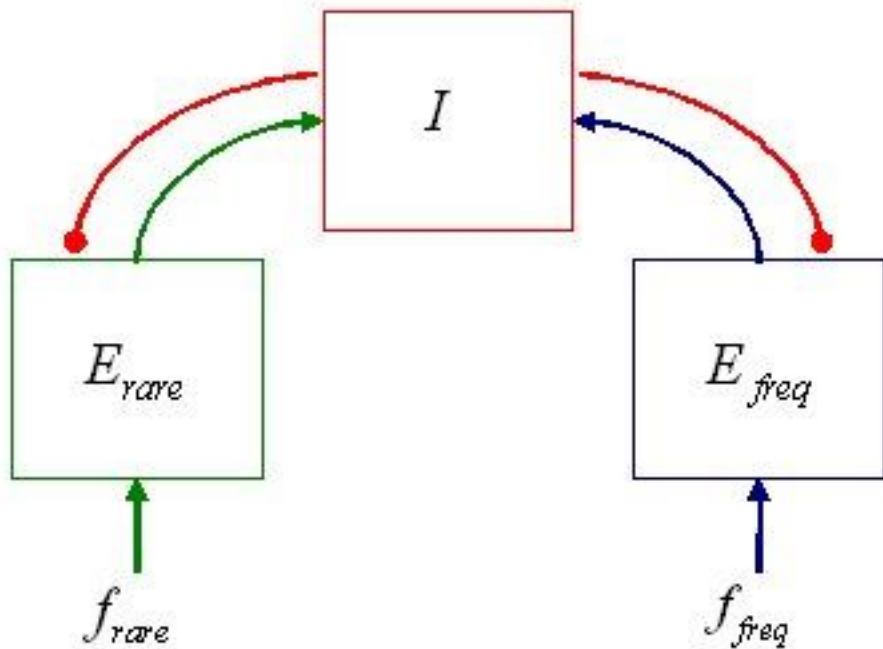
Figure 11: Fixed point loci for networks with tonic activity

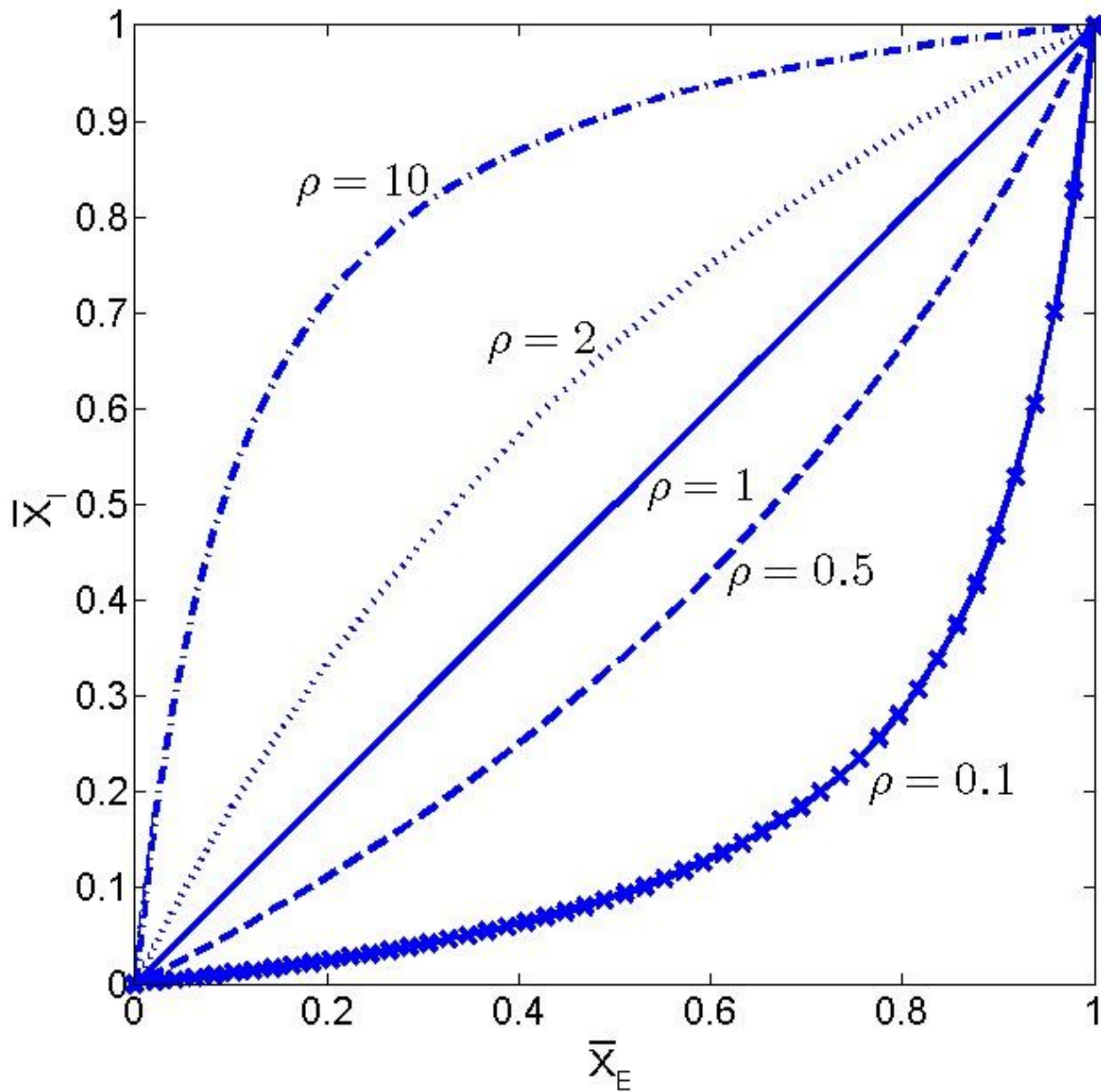
Geometrical loci of fixed points for the system with activity functions described in (17). The locus depends on the parameter ratio ρ following (18). Note the difference between the phase plane structure in this system and the phase plane presented in Figure 2. The difference is due to the different relationships between inhibitory and excitatory activity (compare (17) and (8)). ($W_{ii} = 0.3$)

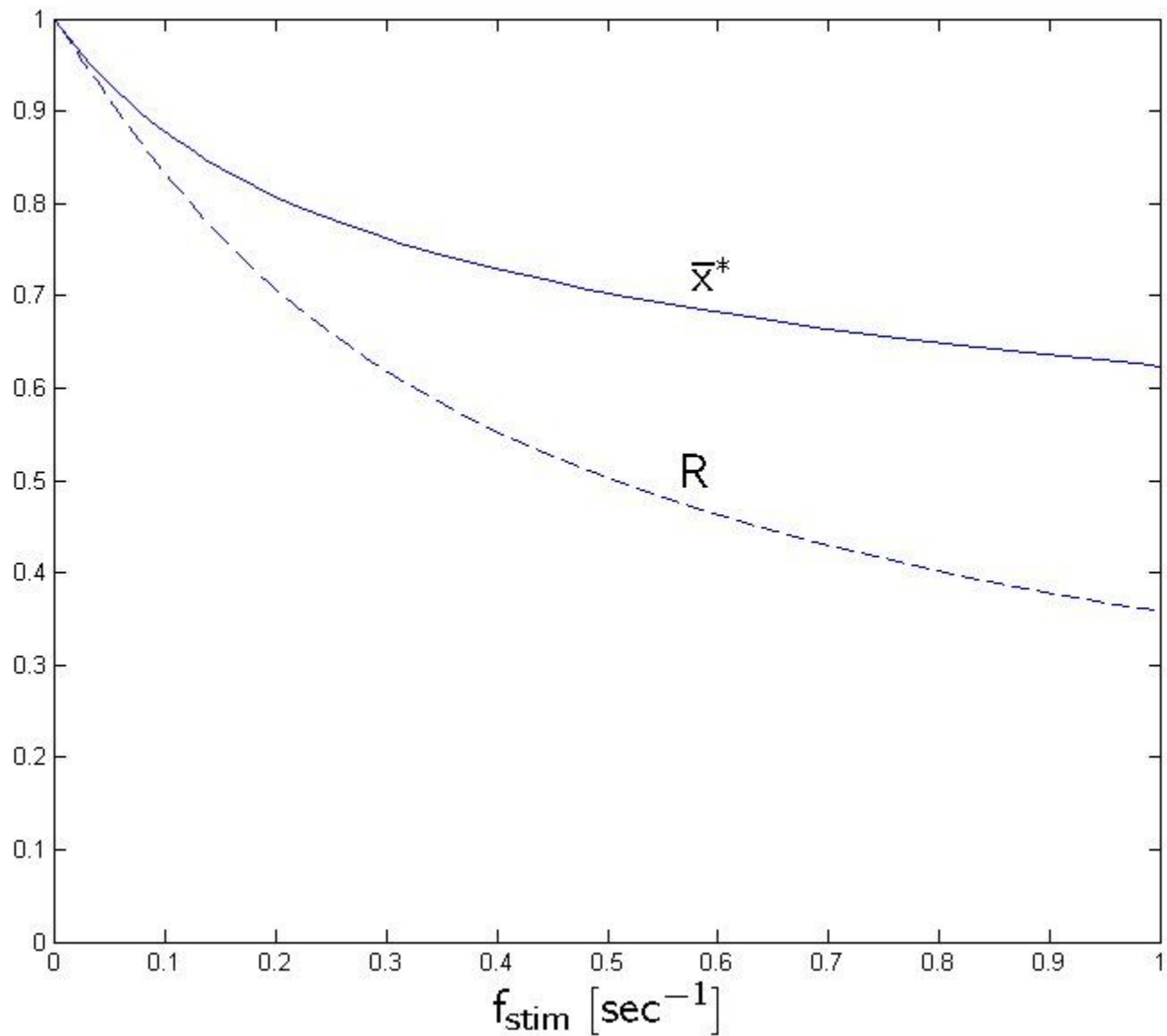
Figure 12: Selective adaptation in networks with tonic activity

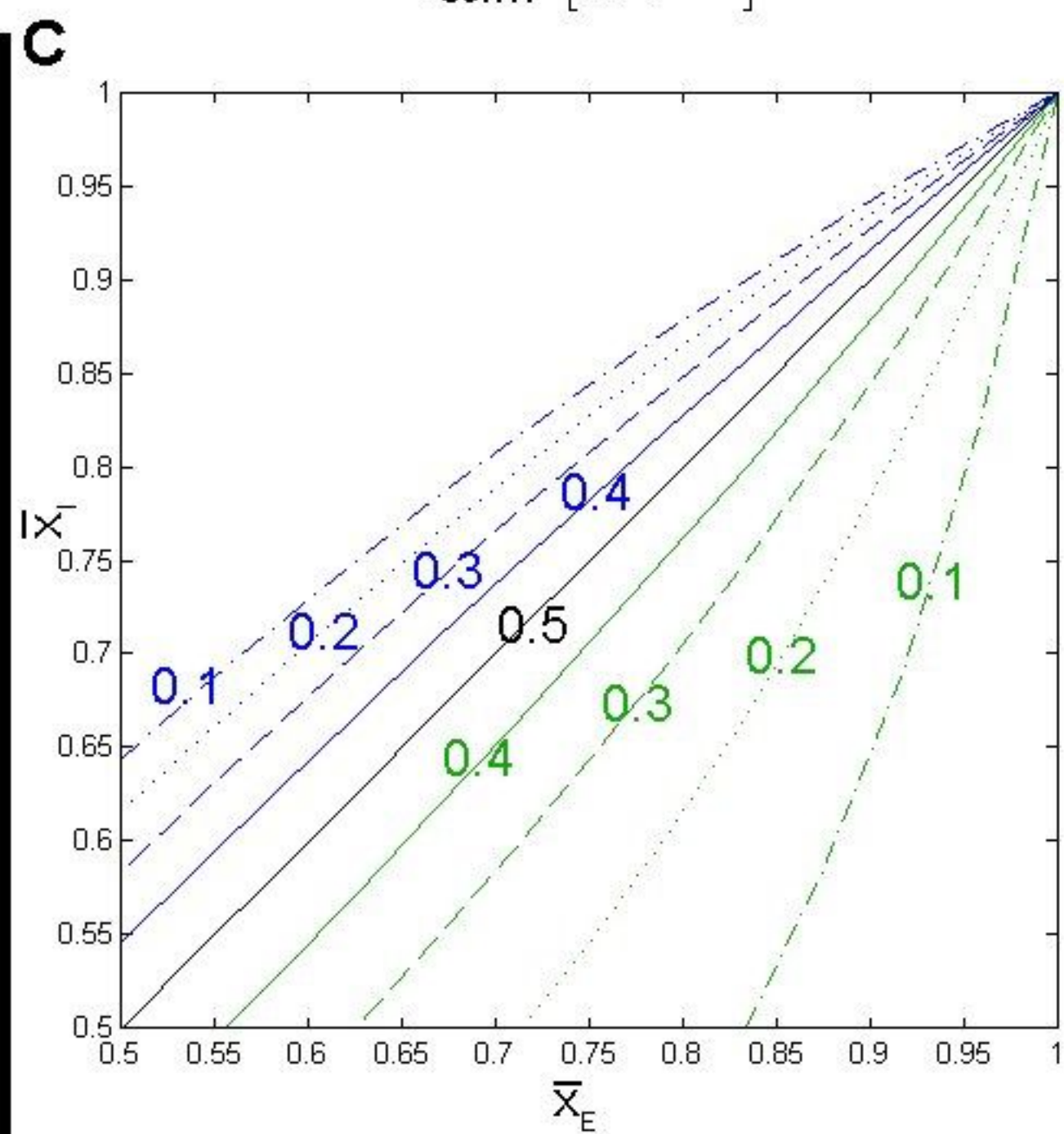
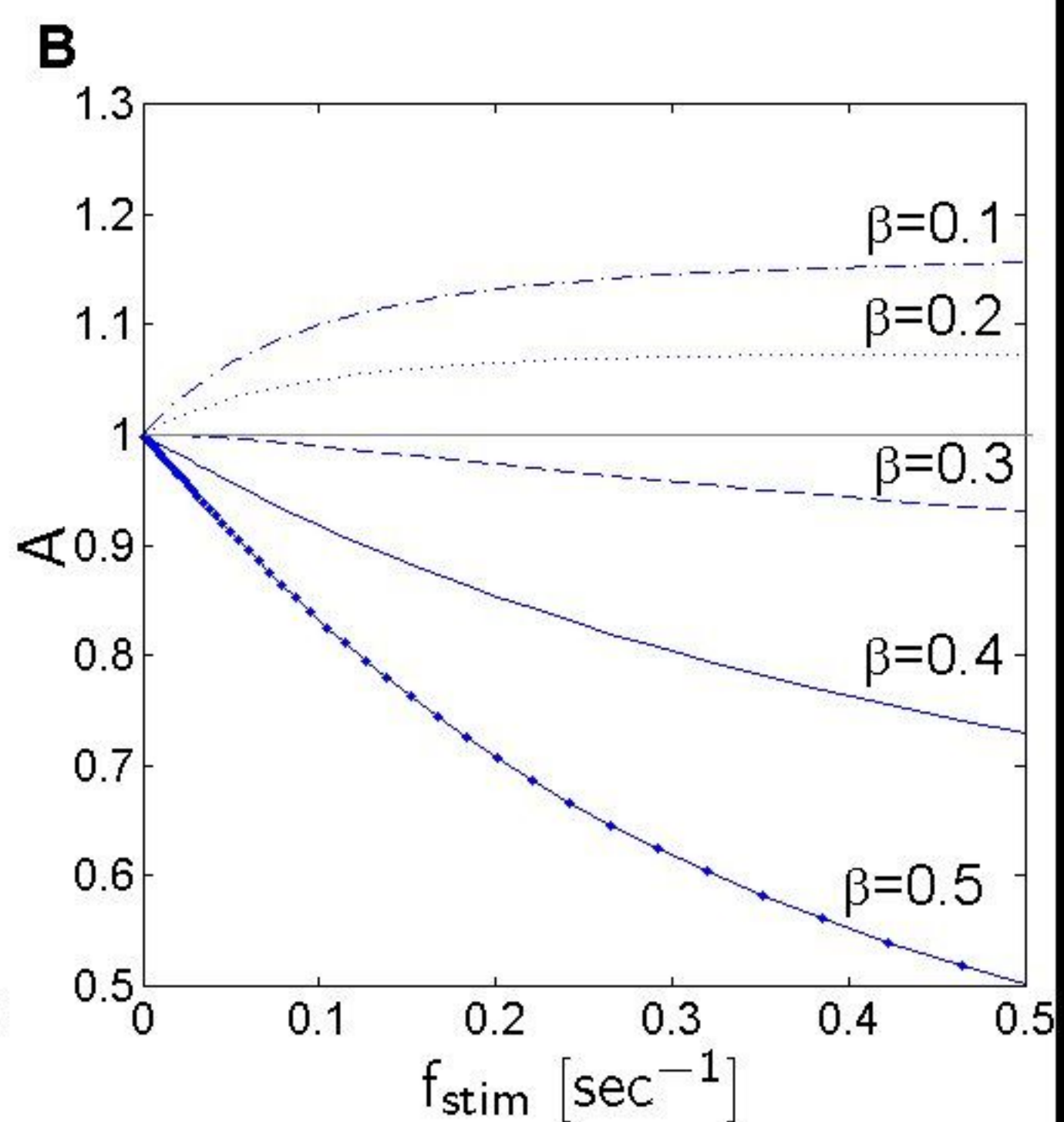
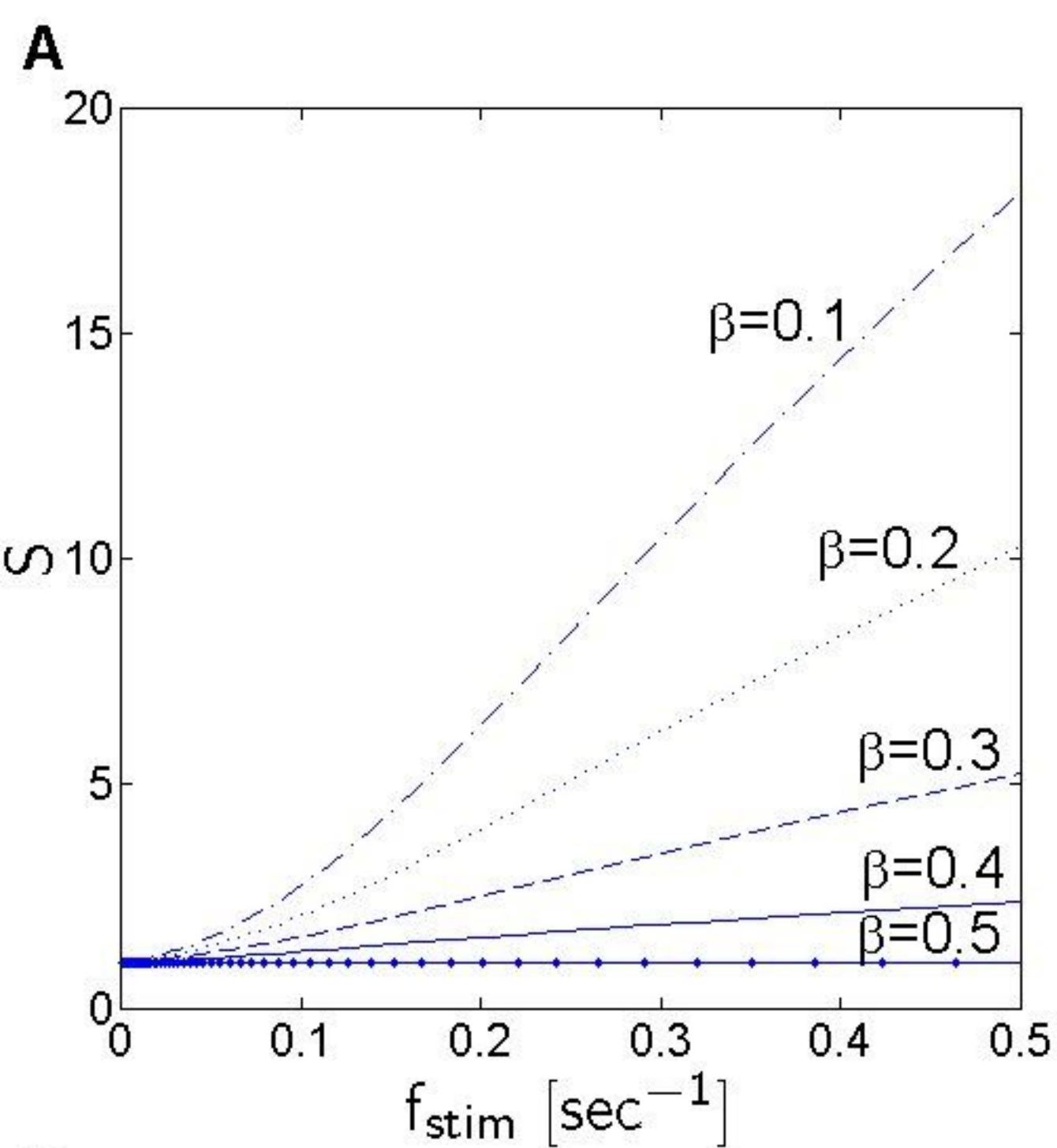
(A) schematic diagram of the dual site stimulation scheme. (B,C) Dependence of selectivity and amplification on total stimulation intensity F_{stim} (logarithmic scale) and relative intensity β . At low intensities response at both sites is high and behavior is similar to the one described for networks with transient responses (see Figure 4). At high intensities responsiveness is low and selectivity and amplification deteriorate. ($W_{ee} = 0.9$; $W_{ei} = 0.75$; $W_{ii} = 0.75$; $W_{ii} = 0.3$)

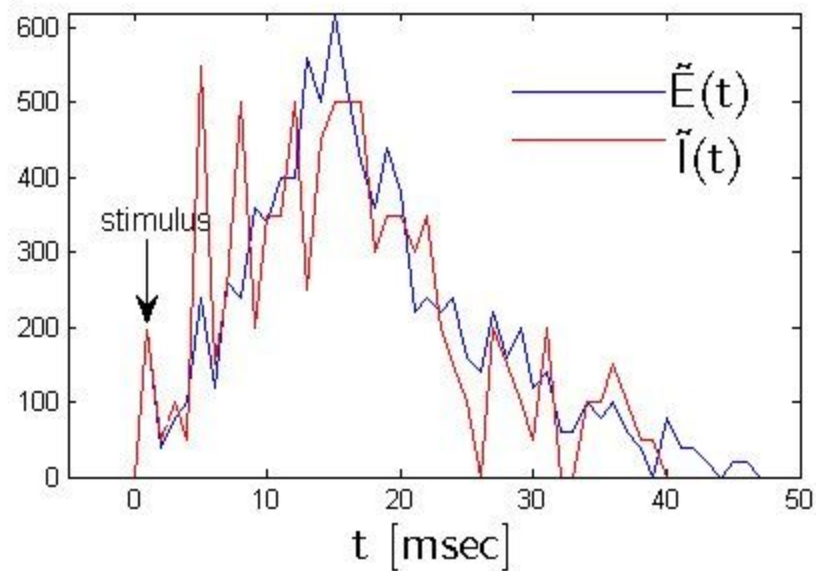
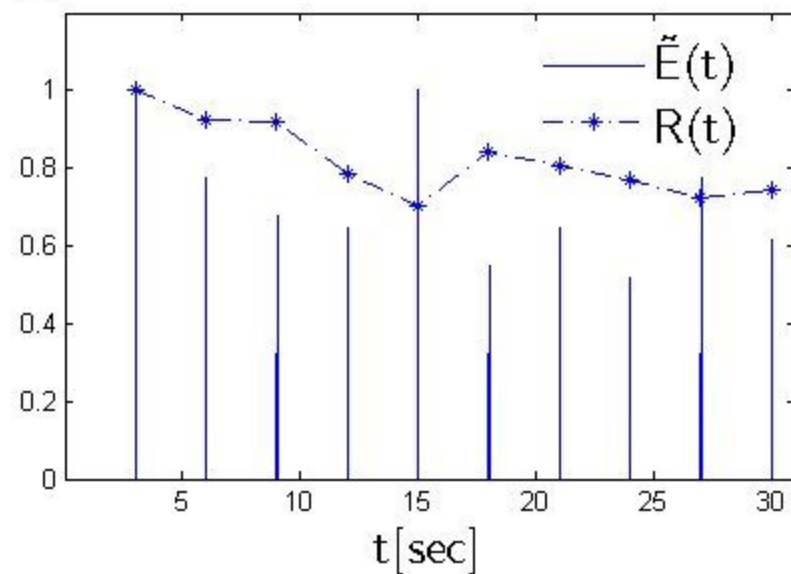
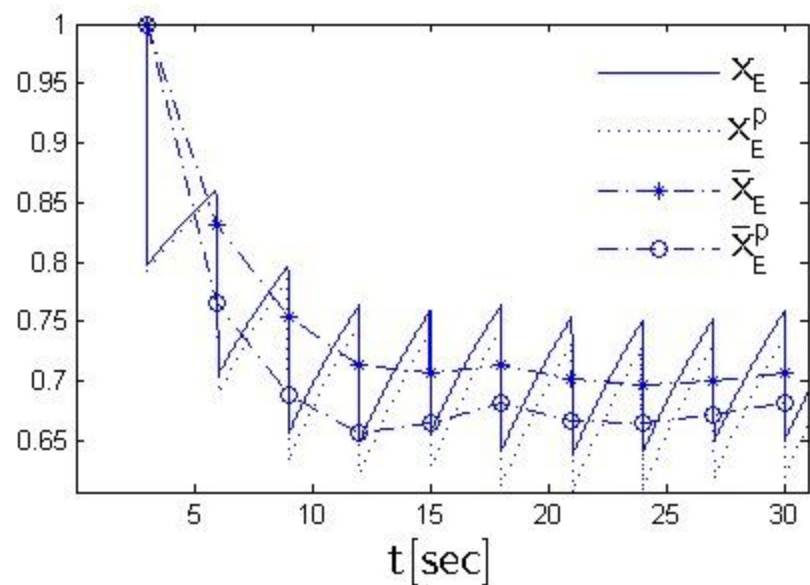
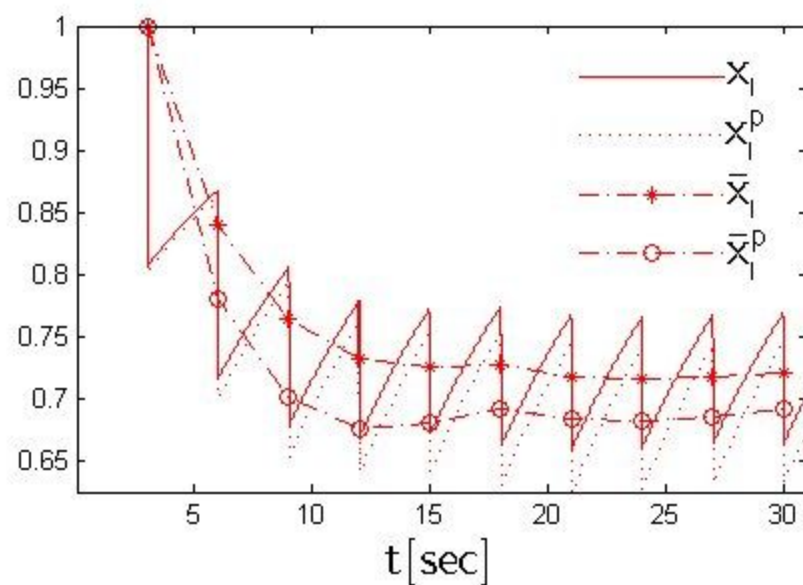
Table 1: Summary of simulation parameter values

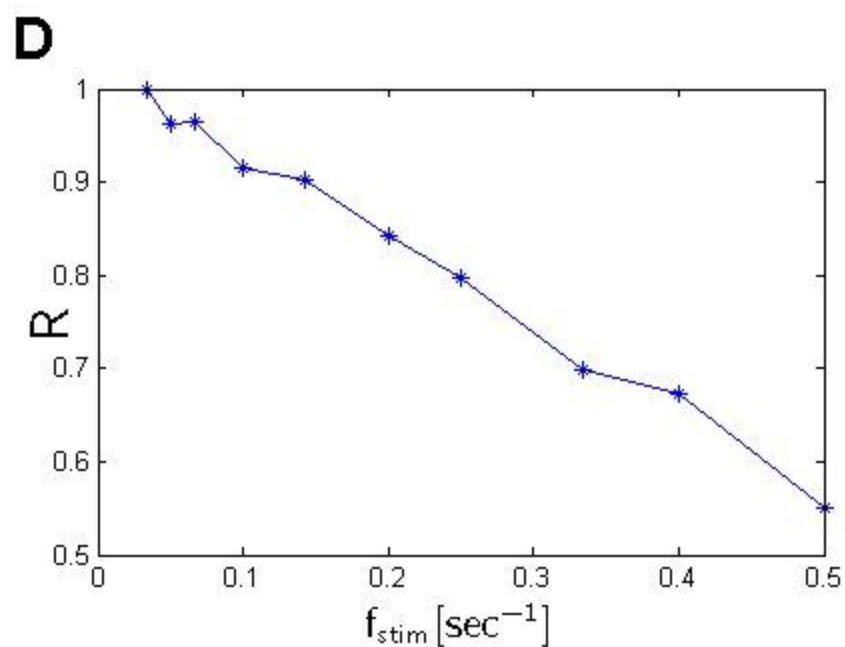
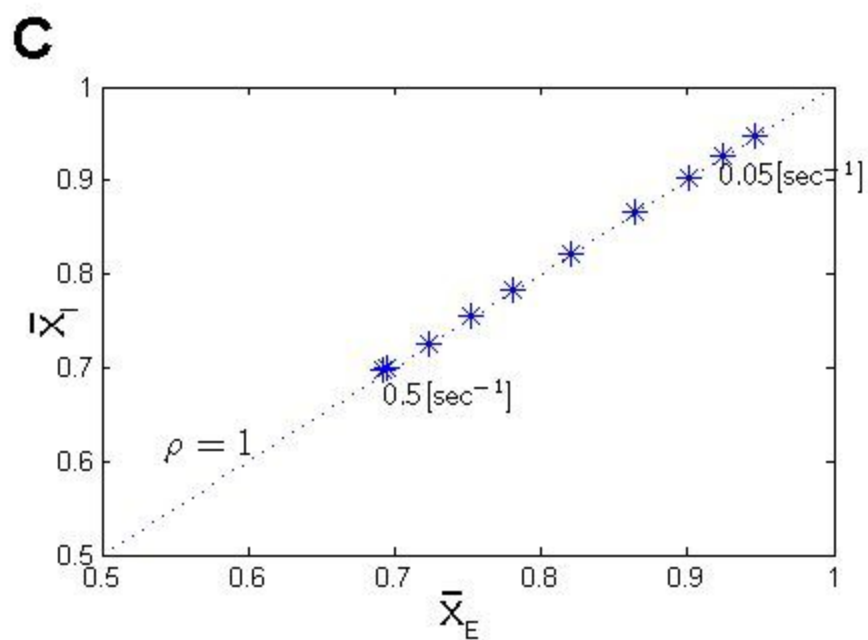
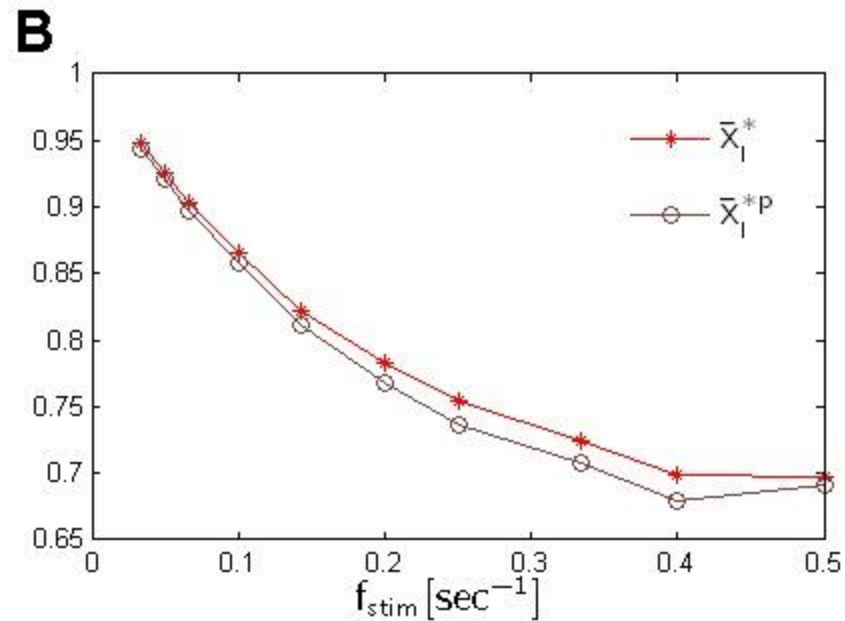
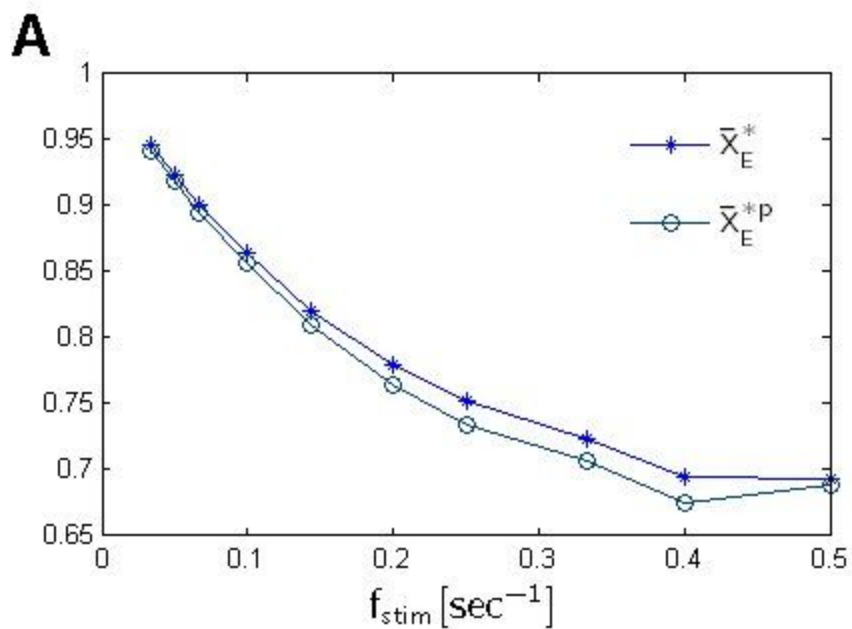


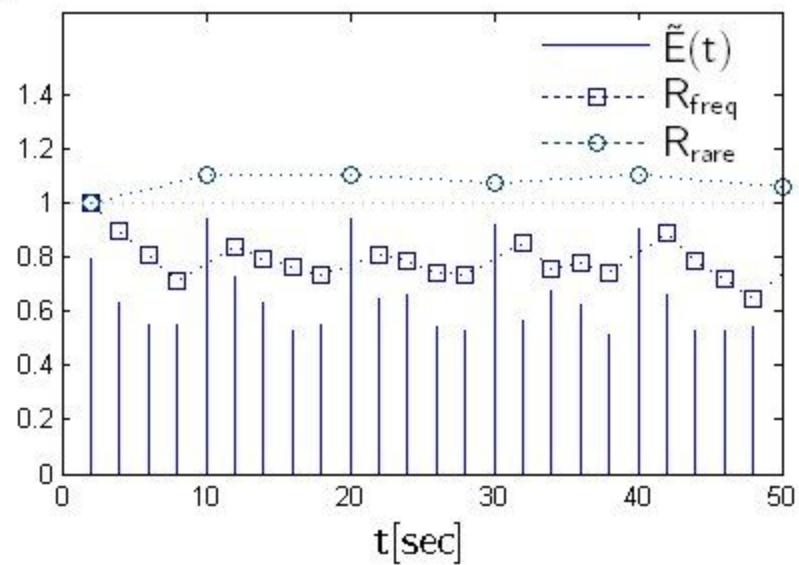
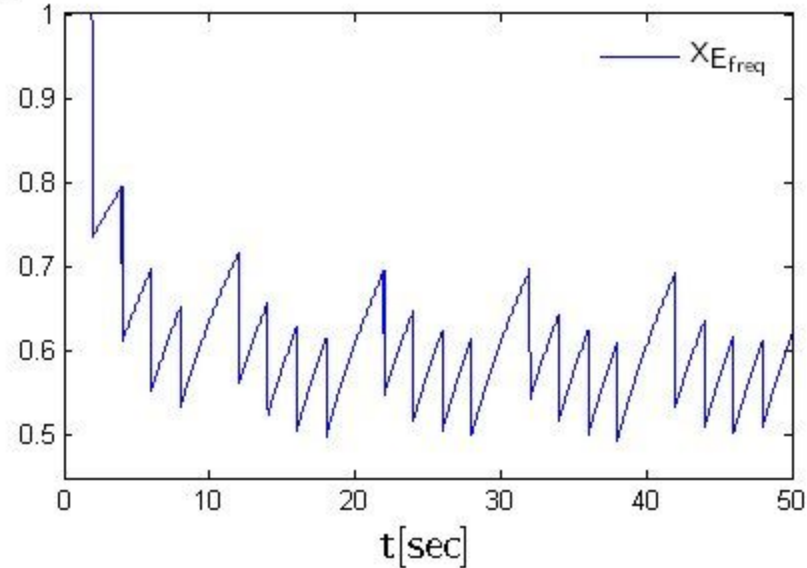
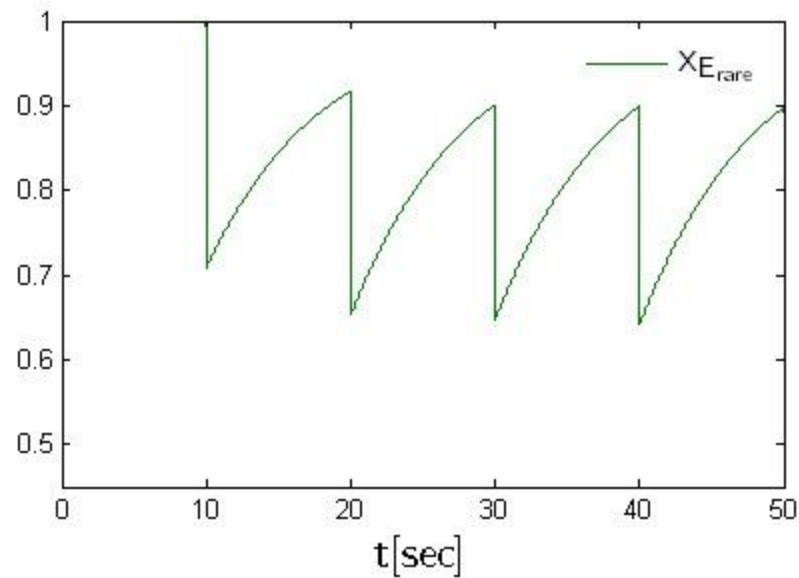
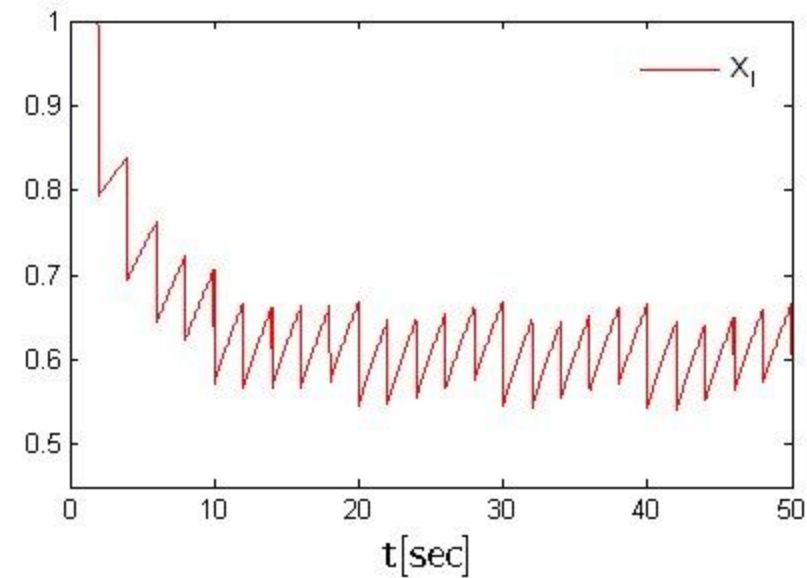


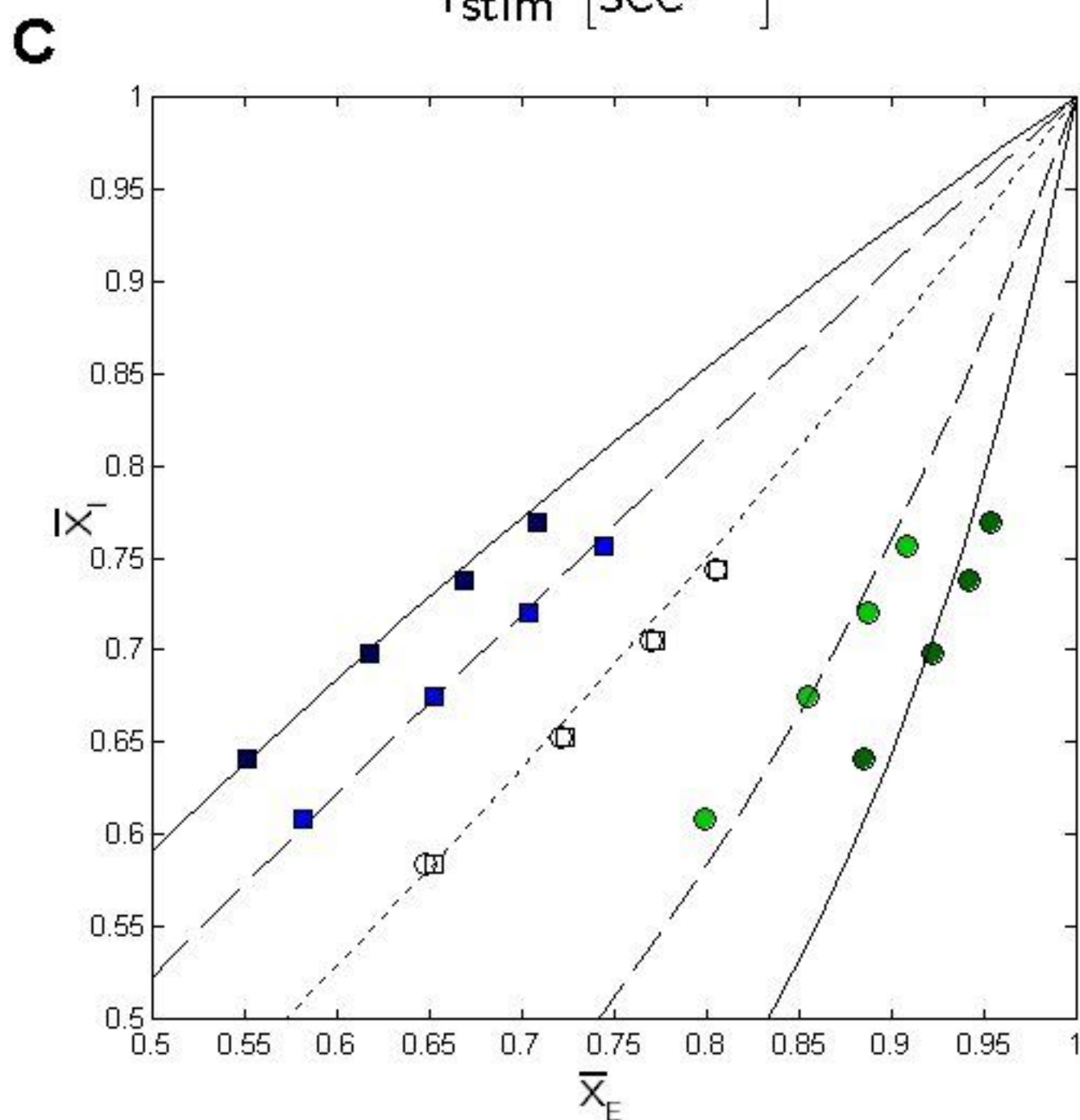
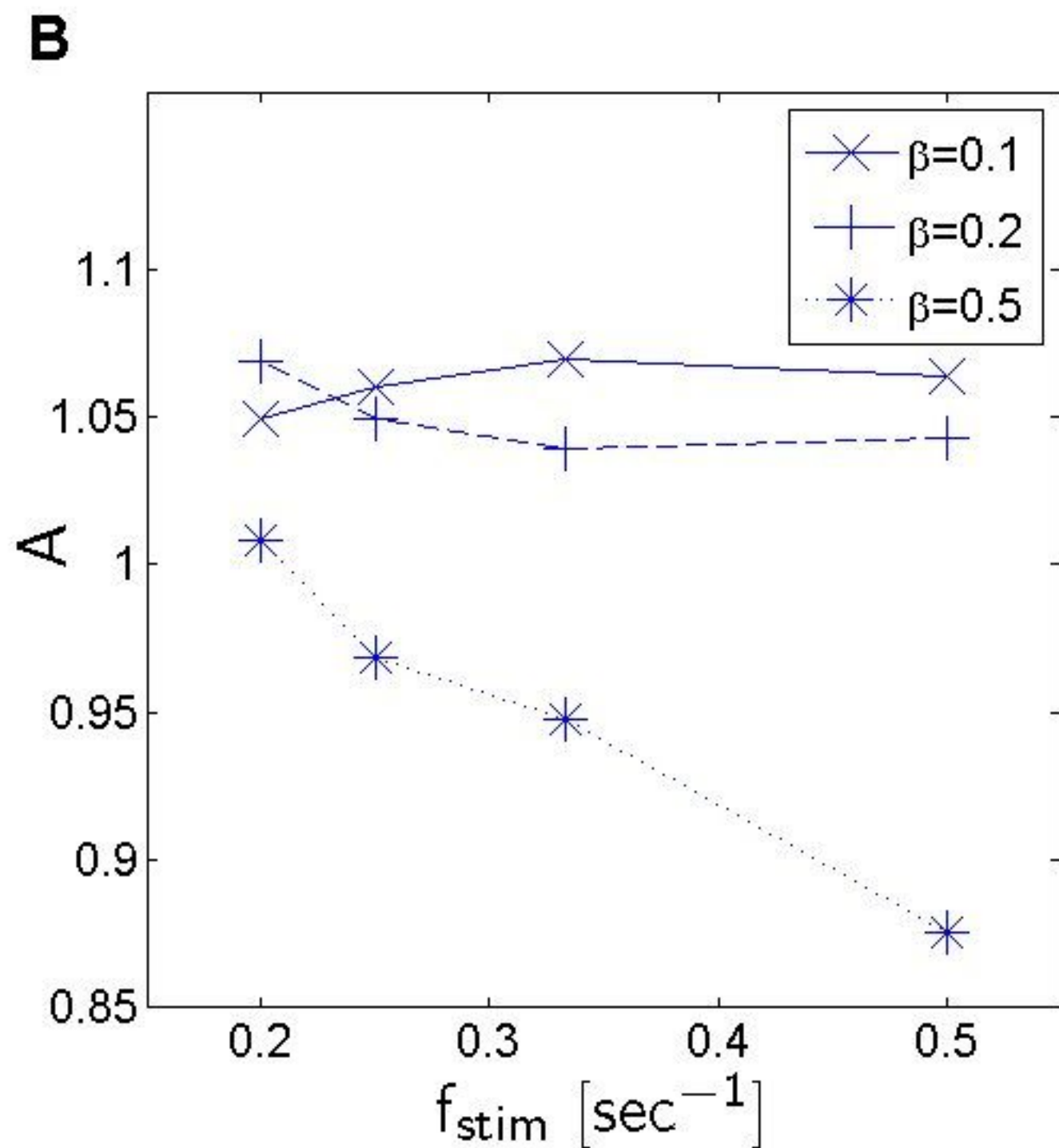
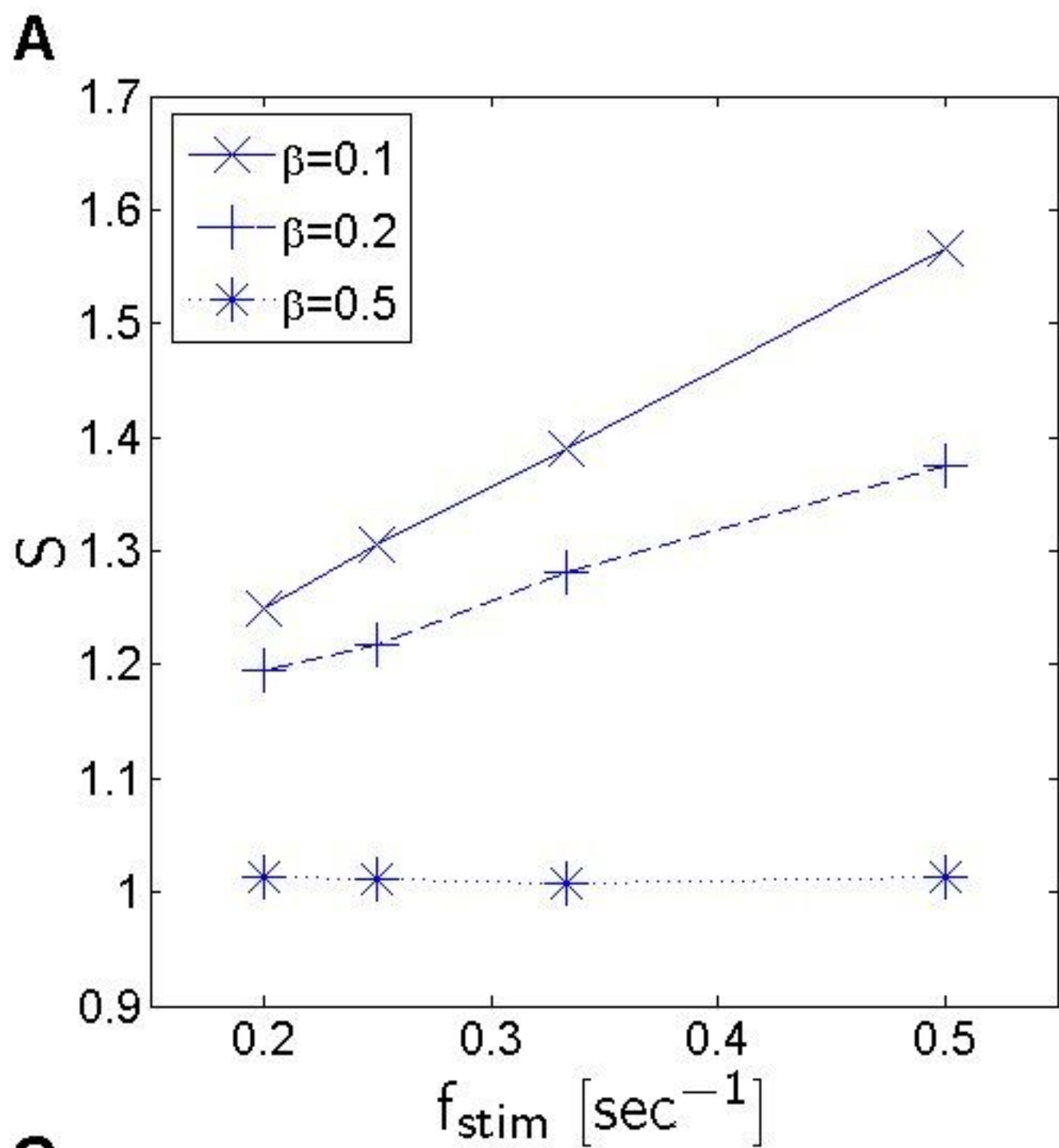


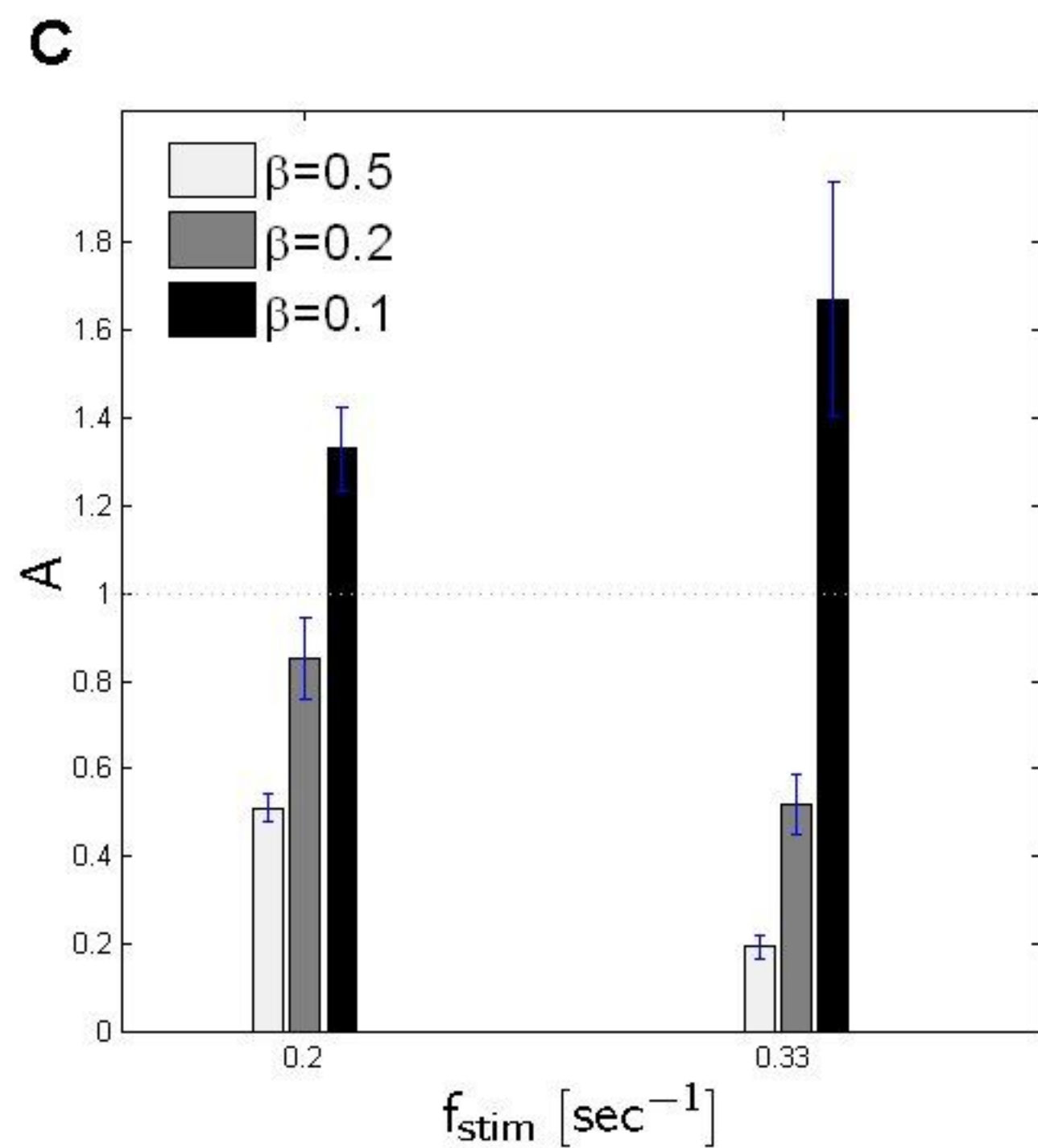
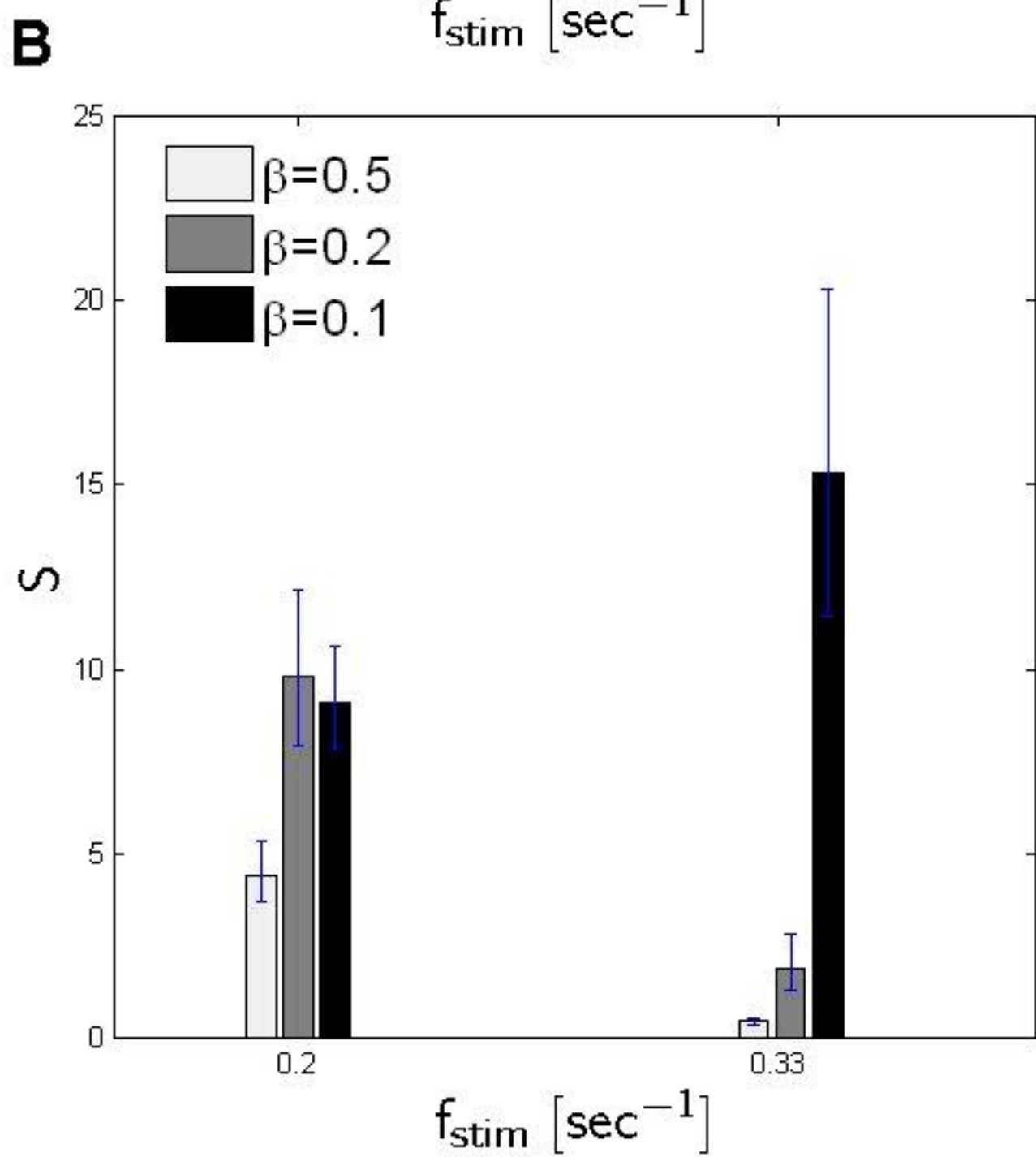
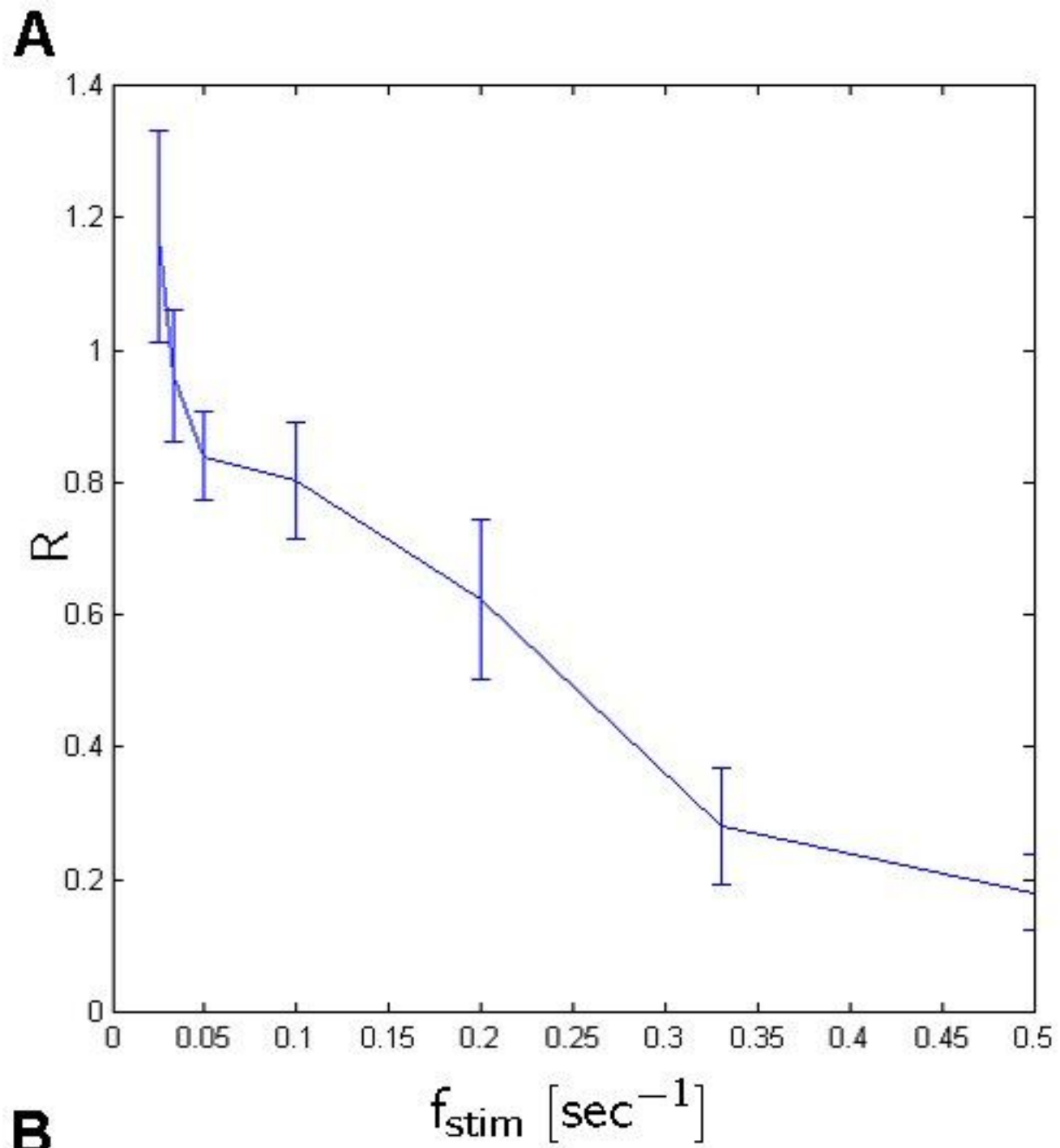


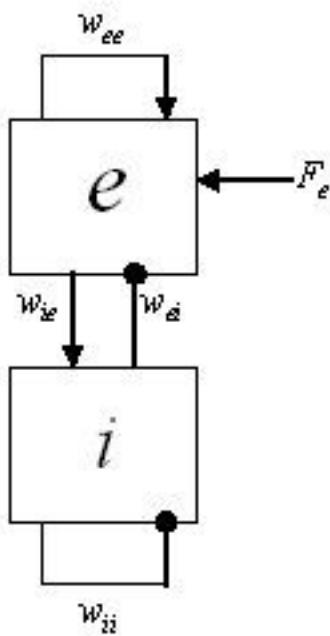
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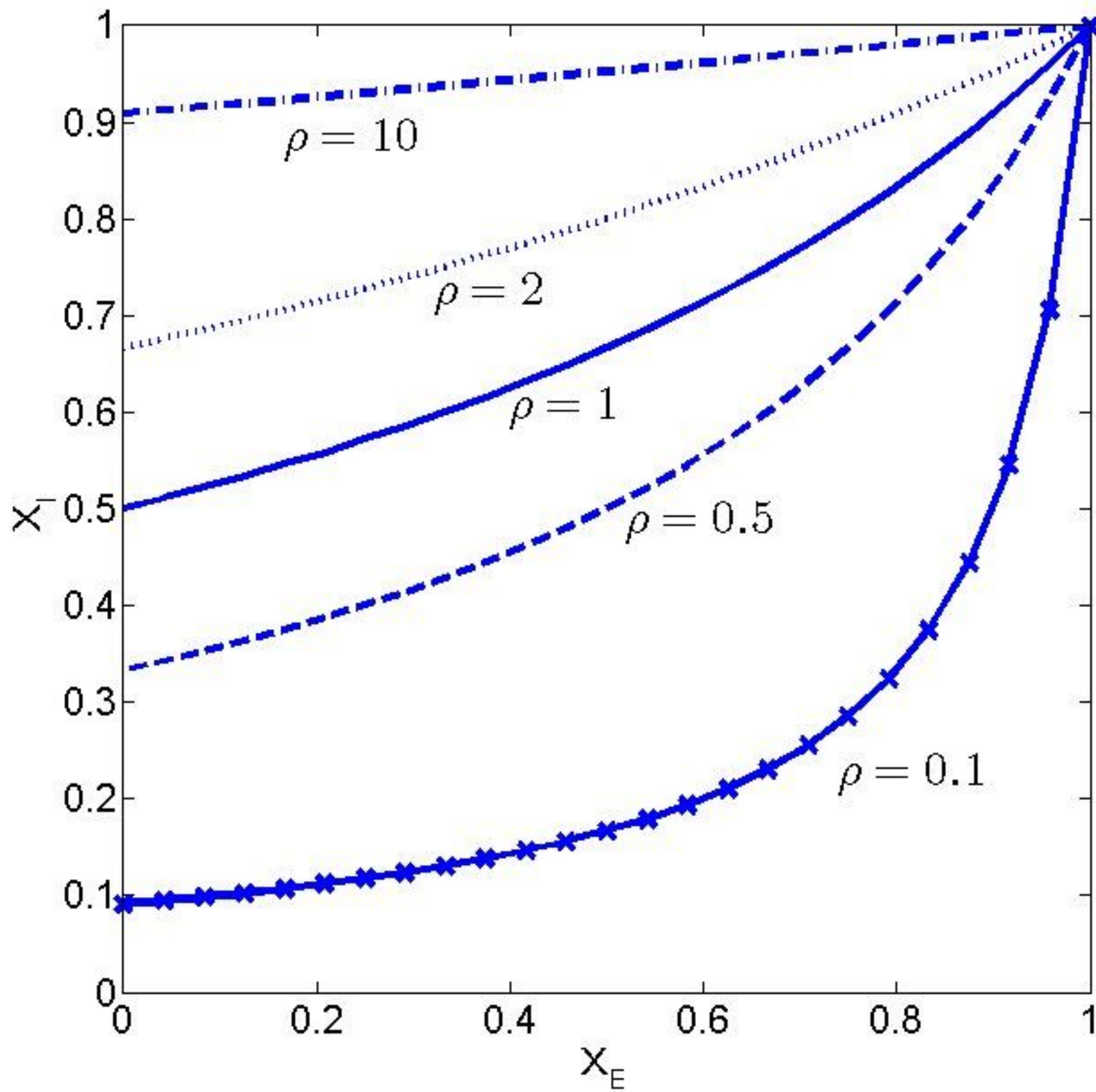


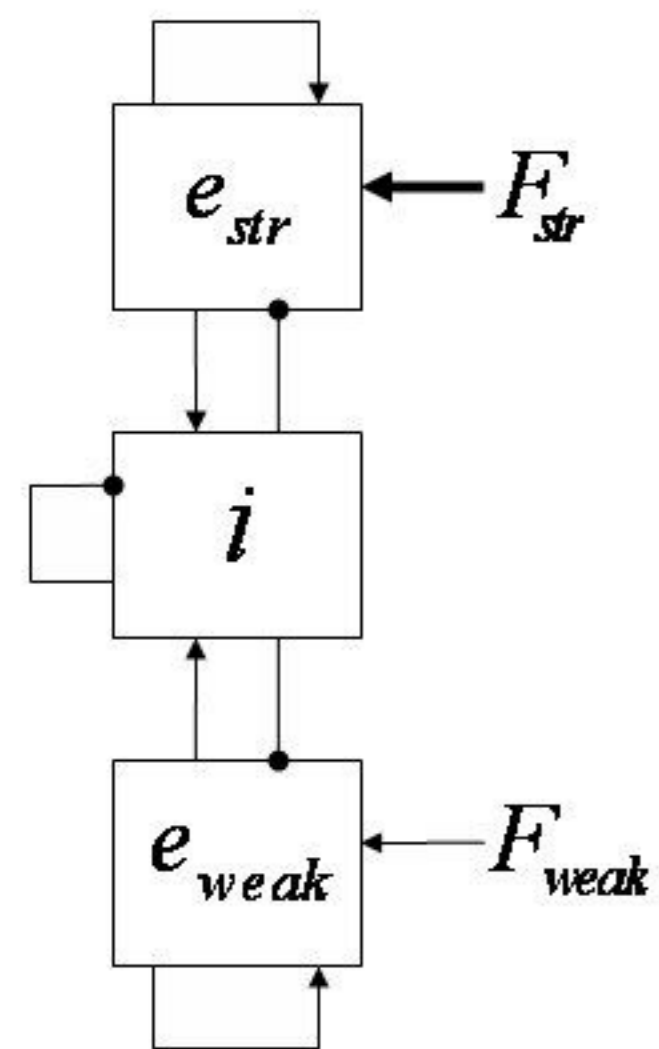
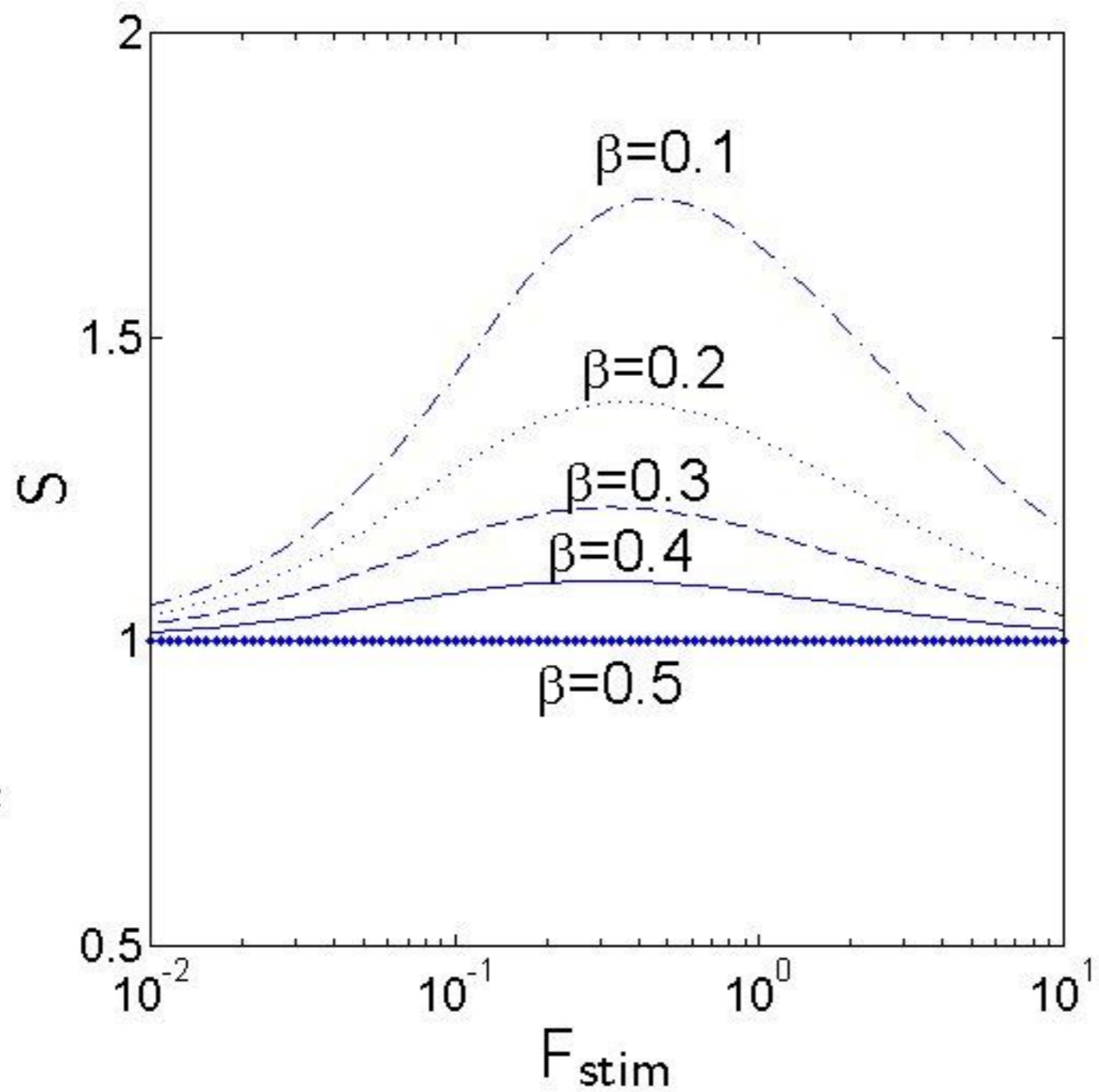
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